Platform Mergers: Lessons from a Case in the Digital TV Market^{*}

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Abstract

This paper contributes to the analysis of mergers in two-sided markets, notably those in which a platform provides its service for free on one side but obtains all its revenues from the other, as in the digital TV industry. Specifically, we assess a decision of the French competition authority which approved the merger of the broadcasting services of the TV channels involved but imposed a behavioral remedy prohibiting the merger of their respective advertising sales services. To do so, we build a structural model allowing for multi-homing of advertisers and, using a comprehensive dataset, we estimate the demand of viewers and advertisers. Our evaluation provides evidence that the remedy has been ineffective at limiting the increase in prices and amounts of advertising, due to the cross-side externalities between viewers and advertisers. Without resulting in significant positive effects on the viewers' surplus, the remedy has also drastically increased the advertisers' total cost. Nevertheless, the remedy has benefited the competitors of the merging channels. The main lesson of our analysis is that, in the process of designing competition or regulatory policy for two-sided markets, ignoring the interaction between the two sides of platforms can result in unexpected outcomes.

JEL Classification: K21, L10, L40, L82, M37

Keywords: Two-sided market, platform merger, advertising, TV market, competition policy

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1 Introduction

Competition authorities have been particularly concerned in recent years by the behavior of dominant firms in two-sided markets, which provide services on one side but generate revenues on the other, in a way that could harm the interest of consumers.¹ In the internet industry, users search the web free of charge, but trigger advertisements which generate revenues for the firms that supply the search engines. Similarly, in the digital TV market, when viewers watch a program for free, they receive a flow of advertisements that generate revenues for the TV channels. Dominant firms in these markets often provide better services than their rivals without charging an extra monetary price to their users. In this way, the dominant firms attract more users, which, in turn, increases their attractiveness in the advertising market. While consumers enjoy a free service from these firms, they may be overwhelmed by the amount of advertising. This can be even more problematic when the dominant firms can offer better services by expanding their customer base, which allows them to show more advertisements (as a non-monetary price) to their users. On the other hand, the acquisition can increase the market power of the merging firms in the TV advertising market, which allows them to charge higher prices to the advertisers.

This paper studies this situation by providing a structural analysis of the acquisition of two new entrants in the French digital TV market, namely, channels NT1 and TMC, by a big media holding company, the TF1 Group. We observe a unique situation in which the French competition authority approved the merger of the broadcasting services of the two purchased channels with those of the acquiring company but blocked the merger of their advertising sales houses (ASHs herein).² In practice, the competition authority imposed a behavioral remedy which requires that the ASH of NT1 and TMC remain separate from that of the main channel of the TF1 Group, namely, channel TF1.³ In this decision, the authority wished to improve the broadcasting quality of the two purchased channels without generating detrimental effects for the advertising market.⁴ To this end, it expected to enhance competition for viewers among TV broadcasters without reducing competition in the TV advertising market.

While the competition authority's examinations of both the broadcasting and advertising sides of the market were straightforward, its decision nevertheless treated the channels' advertising services separately from their broadcasting services. We show in this paper that ignoring the interaction between the two sides of the market can result in unexpected outcomes.

Using a comprehensive dataset on the French digital TV market, covering two years of the pre-acquisition period and three years of the post-acquisition period, we first provide reduced-form evidence that the French TV market is a two-sided market. In other words, we show that cross-side network externalities between viewers and advertisers do exist. Based on the assumption that TV channels are two-sided platforms, we then build a structural model which describes the demand functions of TV viewers and advertisers as well as the objective of the ASHs.

TV viewers' preferences between different channels are approximated by a nested logit model. Thanks to data about the genres of broadcasting content, we take care to solve the endogeneity issues related to this type of model. Our estimates of demand elasticities with respect to the amount of advertising indicate a median loss of audience of about 8.7 percent in response to a 10 percent increase in advertising time, suggesting that the negative externalities that advertisers

¹See for instance the European Commission decision, in March 2019, to fine Google 1.49 billion euros for abusive practices in online advertising.

²An ASH handles and sells the advertising time available on the TV stations that it works for.

 $^{^{3}}$ Note that the advertising time of channels NT1 and TMC were already managed by one common ASH before the TF1 Group had acquired these two channels.

⁴More details about the merger decision are provided in Section 5 of the paper.

generate for TV viewers are relatively large.

Our novel approach to model the demand of advertisers considers their multi-homing behavior and allows us to estimate, using aggregated advertising data, whether a channel is a substitute or complement to another channel for advertisers.⁵ In more detail, we model the advertisers' objective as one that minimizes the total advertising costs which generate the desired audience, and estimate the advertisers' cost function approximated by a translog model. We find that the advertisers consider the two purchased channels (NT1 and TMC) as substitutes, but both as complements of channel TF1. This demand pattern of advertisers implies that merging the ASHs of the three channels would not result in a significant increase in the price of advertising.

Based on the estimates of the model parameters, we evaluate the consequences of the acquisition. Using post-acquisition data, we first show that the broadcasting quality of the two purchased channels has increased, but the ASHs reacted to the changes in the broadcasting quality of TV channels by adjusting their amounts (and hence the prices) of advertising. By counterfactual simulation, we then show the following: i) in the absence of the negative externalities that advertisers generate for viewers, the ASHs respond to the increase in willingness of advertisers to pay for the advertising slots of the merging channels (as a result of the increase in their broadcasting quality and therefore their viewership) by restricting their total amounts of advertising slots and thereby increasing their prices; ii) the two-sided network externalities between viewers and advertisers further incentivize the ASHs to increase the amount of advertising on the merging channels following the increase in their broadcasting quality since viewers are less sensitive to the amount of advertising during programs of better quality; iii) the joint effect of the changes in broadcasting quality and the two-sided network externalities results in an increase in both the amounts and prices of advertising of the merging channels.

To gain an insight into the potential consequences of merging the ASHs of the three channels, we simulate the equilibrium amount of advertising and its price in the case in which the advertising time of NT1, TMC and TF1 is chosen and sold by one common ASH. We show that merging the ASHs of the three channels would only slightly increase their total advertising, due to the small substitution effect of advertising on the viewers' side, and would have almost no impact on the price of advertising, since the slots of the two merged ASHs are complements for advertisers. A welfare analysis further suggests that blocking the merger of the ASHs of the three channels did not have a significant positive effect on the surplus of TV viewers, but has increased advertisers' total advertising cost. At the same time, we note that the behavioral remedy has benefited the ASHs of TF1 Group's competitors by avoiding an important shift of the total advertising profits from the non-merging ASHs to the merging ones. On the basis of European competition law, the French competition authority should have approved the merger of the ASHs of the three channels, since the consumer surplus remained almost unchanged. However, in the political debate, a decision about whether to approve this merger could be determined according to the weights that the people allocate to the different market players. In any case, the two-sided nature of the market should not be ignored when examining the merger.

This paper first contributes to the relatively limited empirical literature on two-sided markets. Beginning with the seminal articles of Rochet and Tirole (2003) and Armstrong (2006), theoretical papers have addressed TV advertising competition by considering the amount of advertising as a nuisance to TV viewers (e.g., Anderson and Coate, 2005; Cunningham and Alexander, 2004; Nilssen and Sørgard, 2000). In practice, very few empirical papers have estimated viewers' demand elasticities with respect to the amount of advertising. Wilbur (2008) finds TV viewers dislike advertising. A similar attitude of viewers towards advertising has also been found in the radio and

⁵We thank the Editor for pointing out the issue of the substitutability between channels for the advertisers.

newspaper industries. (See Jeziorski, 2014; Ivaldi and Muller, 2018.) However, empirical studies have also found audiences appreciating advertising in yellow pages and magazines. (See Rysman, 2004; Kaiser and Wright, 2006; Ivaldi and Muller, 2018.) Here, identifying the sign of the network externalities that the advertisers generate for viewers is crucial, as it impacts the strategic behavior of the ASHs in the advertising market. If viewers dislike advertising and switch channels during the advertisements, the ASHs would restrict the amount of advertising on TV to avoid losing viewers, but would increase the amount of advertising on a TV channel following an increase in its broadcasting quality. In our estimates, we find a statistically significant disutility of advertising to TV viewers.

This paper also contributes to the extensive literature on mergers. Post-merger analysis has been adopted to evaluate the effectiveness of competition policy in numerous industries, such as airlines (Borenstein, 1990; Kim and Singal, 1993), banking (Facacelli and Panetta, 2003), petroleum (Hastings, 2004; Gilbert and Hastings, 2005; Hosken, Silvia, and Taylor, 2011), and appliances (Ashenfelter, Hosken, and Weinberg, 2013). Ashenfelter and Hosken (2010) assess mergers in five different branded-goods industries. Björnerstedt and Verboven (2015) evaluate the performance of merger simulations in the Swedish analgesics market. In line with the previous literature, we evaluate the ex-post consequences of an approved acquisition under behavioral remedy in the digital TV market. Our structural analysis is also related to another branch of the merger literature that quantifies the welfare effects of mergers. Examples of such articles include Baker and Bresnahan (1985), Hausman *et al.* (1994), Werden and Froeb (1994), and Nevo (2000), among others.

More recent literature is interested in the effects of mergers in two-sided media markets, and in particular on the product positioning that Sweeting (2010) has initially studied in detail in the context of the radio industry. Fan (2013) simulates the potential consequences of a merger prohibited by the Department of Justice in the US newspaper industry. She develops a model which endogenizes the choice of characteristics and shows that ignoring adjustments of product characteristics causes substantial differences in estimated effects of mergers. Jeziorski (2014) evaluates the ex-post welfare effects of mergers in the US radio market. In particular, he decomposes the changes in consumer surplus into product repositioning effects and advertising quantity readjustment effects. He shows that the product repositioning effect of a merger improves listeners' surplus but the resulting advertising readjustment reduces it. Our data are not sufficiently disaggregated to allow us to study the repositioning of products after the merger. However, we show the key role of the quality of broadcasting services alongside that of two-sided network externalities in determining the magnitude of the impact of the merger in our study.

The remainder of this paper is structured as follows. In Section 2, we present the French digital TV market. In Section 3, we model the demand of TV viewers and of advertisers. The demand estimates are presented in Section 4. We carry out the merger evaluation in Section 5 and conclude in Section 6.

2 The French digital TV market

2.1 Data

The Conseil supérieur de l'audiovisuel (the French audiovisual regulator, CSA herein), has made available to us the monthly audience and advertising data of 12 major broadcast TV stations in France from March 2008 to December 2013. The sample is representative of the French TV market: The total audience share of the 12 stations exceeds 95 percent of the free-broadcast TV market and 79 percent of the whole TV market including pay TV; the total advertising revenue share of the 12 stations exceeds 90 percent of the free-broadcast TV market and 81 percent of the whole TV market. The list of the 12 TV stations is provided in Table 1. All 12 TV stations are generalist, broadcasting a wide range of programs. The incumbent channels have been broadcasting since 1950, while the new channels entered the market in 2005. The three channels involved in the acquisition (as mentioned in the Introduction) are highlighted in bold.

	Channels	Nature	Media Group membership
			1 1
Incumbents	$\mathbf{TF1}$	$\mathbf{private}$	TF1 Group
	M6	$\operatorname{private}$	M6 Group
	FR2	public	FTV Group
	FR3	public	FTV Group
	FR5	public	FTV Group
New entrants	NT1	private	TF1 Group
	\mathbf{TMC}	private	TF1 Group
	W9	$\operatorname{private}$	M6 Group
	FR4	public	FTV Group
	D17	private	Canal plus Group
	D8	private	Canal plus Group
	Gulli	$\mathbf{private}$	Lagardère Group

Table 1: List of TV channels and their ownership since 2010

The audience data come originally from Médiamétrie, which builds a measure of audience by recording the television usage every second by a panel of households equipped with one or more TV sets in their main residence.⁶ From these raw data, we derive our monthly measure of audience as a weighted average of viewers per second in a month.⁷

The advertising data – more precisely, the gross advertising revenues and the number of advertising seconds – come from Kantar Media. Using this information, we estimate the monthly average advertising price per second by dividing each channel's gross advertising revenues by the number of seconds of advertising in the month. This is the price that the ASHs charge advertisers in our model.

Table 2 presents summary statistics of the main variables in our analysis. The total number of TV viewers per channel per second is on average equal to 3.84 thousand. A TV channel broadcasts on average 56 hours (i.e., 0.2 million seconds) of advertising per month. The average advertising price is 5.96 euros per second. These three main variables are measured at the monthly level for each channel.

In addition to the above data provided by the CSA, Médiamétrie supplied us with complementary information on the broadcasting content of the 12 TV stations in our sample. In more detail, we observe the monthly broadcasting hours of six major genres of TV shows per channel per month

⁶This panel has been built to account for both the socio-demographic characteristics of households in metropolitan France and the structure of the television supply. It is made up of nearly 4,300 households, which corresponds to approximately 10,500 individuals aged 4 and over. In each home, Médiamétrie installs one or more audimeters (depending on how many pieces of equipment there are) fitted with a remote control with individual keys, which constantly record all uses of the television set(s) in the household and all the viewing habits of each member of the household and their guests. (See http://www.mediametrie.fr.)

⁷In practice, the number of viewers of channel j in month t, y_{jt} used in the model later, is defined as follows. Médiamétrie measures the number of viewers of channel j at each second s. Assuming there are 30 days in month t (so in all, 2,592,000 seconds in the month), the monthly average number of viewers of channel j, y_{jt} , is equal to $\frac{\sum_{s=259200}^{2592000} y_{js}}{2592000}$, where y_{js} denotes the total number of viewers of channel j at second s. In other words, y_{jt} denotes

 $[\]sum_{s=25000}^{s=25000} \frac{y_{js}}{2592000}$, where y_{js} denotes the total number of viewers of channel j at second s. In other words, y_{jt} the average number of viewers per second of channel j in month t.

Table	2:	Summary	statistics
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Variable	Mean	Std. Dev.	Min.	Max
Number of TV viewers (in thousands)	3.84	4.14	2.86	16.03
Number of seconds of advertising (in millions)	0.20	0.09	0.03	0.44
Advertising price per second (in thousands)	5.96	8.01	0.42	35.95

Note: The total number of observations is 840, which amounts to 70 monthly observations per TV channel. Source: Médiamétrie & Kantar Media.

during the period of study (i.e., 2008–2013). Summary statistics on the broadcasting of the six program genres are provided in Table 3. TV series/movies, culture/science, and entertainment are the most broadcast genres, which occupy more than 70 percent of the broadcasting time of each TV station. The broadcasting of news varies significantly from channel to channel: the new entrants such as TMC, Gulli and D17 do not show any news. Sports and cartoons occupy relatively small shares of the total broadcasting time of the 12 generalist TV stations in our sample; in particular, FR5 and TMC do not show sports, while D8 and W9 do not show cartoons.

Table 3: Monthly broadcasting hours of different genres

Genre	Unit	Level	Man	Stv.	Min.	Max
TV Series/Movies	hours	channel/month	283.85	157.30	16.78	696.00
$\operatorname{Culture}/\operatorname{Science}$	hours	$\operatorname{channel}/\operatorname{month}$	153.23	156.77	2.70	711.45
${\it Entertainment}$	hours	$\operatorname{channel}/\operatorname{month}$	123.41	137.39	0	692.67
News	hours	$\operatorname{channel}/\operatorname{month}$	52.31	53.66	0	214.47
Sports	hours	channel/month	14.31	19.45	0	166.80
Cartoons	hours	channel/month	1.30	2.35	0	21.13

Source: Médiamétrie

2.2 Market structure

TV stations could be considered as two-sided market platforms connecting viewers to advertisers. They provide two services: TV shows to viewers on one side, and advertising slots to advertisers on the other. While viewers enjoy the news and entertainment content on TV, they receive the flow of advertising. When TV viewers see the advertisements, this generates an audience for the advertisers. TV viewers may, however, be sensitive to the amount of advertising, in which case the advertisers generate externalities for the TV viewers. Advertisers value TV advertising for its ability to inform and/or persuade viewers of the merits of products or services they have to commercialize. Therefore, a priori, the more popular a TV channel is among viewers, the more demanded it is by advertisers. Our empirical analysis below provides evidence on the sign and the magnitude of these externalities between the two sides of TV stations.

Advertisers buy the advertising slots of TV channels from the ASHs, whose role is to handle and sell the advertising time available on different TV stations. The ASHs charge advertisers a price per second of advertising that warrants a certain level of audience. The advertisers' objective is then to minimize their total advertising costs by combining the advertising slots on several TV channels in order to achieve a certain overall reach of audience. In other words, the advertisers practice multi-homing strategies. TV programming is decided by the TV channels several months in advance. Based on the broadcasting content provided by the TV channel, each ASH determines its optimal supply of advertising slots. The amount of advertising of a broadcast TV station is, however, subject to two regulation caps enforced by the French law, at the hourly and daily average levels.⁸ In Table A1 in Appendix A, we compare the effective amount of advertising to the maximum minutes of advertisements per month allowed for each TV station (calculated based on the daily average level of the regulation cap); we note that the observed advertising time of different TV channels is well below the regulatory ceilings.^{9,10} The ASHs behave as Cournot-type firms, since they adjust the amount of advertising according to the quality of the TV program and the sensitivity of viewers to the amount of advertising. At equilibrium, each ASH's objective is to determine the optimal amount of advertising in each channel under its management to maximize the sum of its profits from all of these channels.

Unlike pay TV channels, which charge subscription fees to their viewers, free-broadcast TV stations only require their viewers to bear the advertising. While the pay TV stations play an important role in the U.S. TV market, they are much less common in France. Although there were between 184 and 207 pay TV channels available in the French TV market during the observation period, neither their total audience share nor their total advertising revenue share exceeds 10 percent.¹¹ In addition, most of the pay TV channels specialize in one theme and target a specific audience (children, young women, etc.), while the 12 major free-broadcast TV stations included in our study are generalist TV channels which aim to serve a wide audience. We group all the pay TV channels into an outside option of our model because the statistics on the audience share of an individual pay TV channel are not available, due to their negligible share of the market.

2.3 Relation between advertising and TV viewership

If the broadcast TV market is a two-sided market, there are two elements that could support this view: the relation between the amount of advertising and the number of viewers; and the relation between the number of viewers and the advertising spending. For an industrial organization to be considered as a two-sided market, we must identify the externalities between the two sides of the consumers, which are here the viewers and the advertisers.

As the cross-side externalities between the viewers and advertisers could play a crucial role in the evaluation of the merger decision that we investigate in this paper, we perform a descriptive analysis to gain insight into the existence and the sign of those externalities, and to show that there is sufficient variation in our data to identify the structural parameters that we will estimate later in the paper.

⁸The average time per hour per day devoted to advertising must not exceed six minutes for public TV channels, nine minutes for the incumbent private channels, and 12 minutes during the first seven years of broadcasting for the new channels launched in 2005. Moreover, the advertising time cannot exceed 12 minutes within any given clock hour for private TV broadcasters and eight minutes for public TV broadcasters.

⁹As we use monthly data in this paper, we computed the maximum minutes of advertisements per month allowed for each TV station from its daily average level of regulation cap imposed by the regulator: The maximum minutes of advertisements allowed for channel j in month t is equal to the maximum minutes of advertisements per day allowed for channel j in month $t \times$ the number of days in month t.

 $^{^{10}}$ Regulatory constraints at the hourly level can be binding during prime time, though our monthly aggregate data does not allow us to explore this. Crawford *et al.* (2017) and Zhang (2019) have studied this issue in detail.

¹¹See for instance the publication of CSA: https://www.csa.fr/Informer/Collections-du-CSA/ Panorama-Toutes-les-etudes-liees-a-l-ecosysteme-audiovisuel/Les-chiffres-cles/

 $^{{\}tt Les-chiffres-cles-de-l-audiovisuel-francais-Edition-du-2nd-semestre-2013}$

Relation between amount of advertising and viewership

To understand whether the amount of advertising has a significant effect on the viewership of TV channels, and the direction of such an effect, we regress the *number of viewers* on the *number of seconds of advertising*, controlling for the broadcasting hours of different program genres and the channel-, month-, and year-fixed effects. The OLS results presented in the second column of Table 4 indicate that a higher viewership is associated with a higher amount of advertising, which is counterintuitive.

The number of advertising seconds is likely to be endogenous, however, because the error term contains unobserved characteristics of channel-time-genre specific program quality, which are correlated with the amount of advertising. We therefore re-estimate the same equation using BLP IVs, namely, the sum of broadcasting hours of news and entertainment programs of the competing channels during the same months. In contrast to the OLS results, we now find a negative correlation between the amount of advertising and the viewership of a TV station, as shown in the third column of Table 4.

Number of vie	wers (y_{jt})
OLS	IV
0.138^{***}	-0.269*
(0.027)	(0.140)
Yes	Yes
840	840
	10.36
	0.298
	OLS 0.138*** (0.027) Yes Yes Yes Yes

Table 4: Relation between amount of advertising and viewership

Note: Standard errors are in parentheses: ***p < 0.01, **p < 0.05, *p < 0.1

Relation between viewership and advertising spending

Another important element which characterizes the broadcast TV market as a two-sided market platform is the occurrence of network externalities that viewers generate for advertisers. Intuitively, advertisers' willingness to pay should be higher for the advertising seconds of a channel which attracts more viewers. Accordingly, we should expect higher advertising spending on the advert seconds with more viewers.

To illustrate this, we present a binned scatterplot of the relation between the *number of viewers* per second and its corresponding advertising spending, i.e., the per second advert price defined in Section 2.1, controlling for channel-, month- and year-fixed effects.¹² The result is presented in Figure 1. Note that a higher viewership is associated with higher advertising spending, suggesting that the TV viewers generate positive network externalities for the advertisers.

3 Demand model

We now present our structural model for the demand of TV viewers and advertisers. We explain here the motivation behind the choice of our specification. Then, in the next section, we discuss

¹²We thank an anonymous referee for suggesting this.

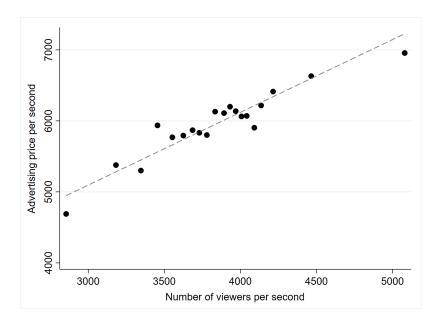


Figure 1: Relation between TV viewership and advertising price

the estimation results for these models.

3.1 Viewers' demand

We specify the viewers' demand using a nested-logit model, which classifies the choices of the TV viewers into g groups (or nests) and an additional group for an outside good. As is well known, one of the main properties of this model is that choices within the same group are closer substitutes than choices from different groups (see Berry, 1994). Our categorization of the groups is motivated by the following considerations.

Our sample includes 12 major broadcast TV stations: five incumbent channels and seven new entrants. We categorize the incumbent channels and the new entrants into two different groups to take into account their different brand awareness, type of content, and quality. The seven new entrants do not enjoy the same market position as the five incumbent channels: The audience shares of the new channels are remarkably lower than those of the incumbents. (See Table A2 in Appendix A for detailed statistics.)

Three elements explain this difference. First, the incumbent channels and new entrants do not have the same brand awareness, simply because they entered the market at different times. The incumbent channels have been broadcasting since 1950, while the seven new channels entered the market in 2005. The new entrants also required a new reception technology, which was only adopted gradually by the French households between 2005 and 2013.

Second, the broadcasting content on the incumbent channels has a different focus and quality from that on the new channels. Although all of the 12 TV stations in our sample show a wide range of genres of programs, the incumbent channels devote relatively more time to news and culture/science, while the new channels show more TV series/movies.¹³ The incumbent channels offer better quality of sports events and entertainment programs than the new entrants: Only the incumbent channels can afford the cost of broadcasting popular sports events such as the Champions League, the Olympic Games, and expensive live shows such as *The Voice*.

¹³See Figure A.1 in Appendix A for the distribution of different genres of program on incumbent and new entrant channels.

Third, a French law requires the free-broadcast TV stations to show at least 40 percent of French audiovisual programs per day. The incumbent channels must fulfill this obligation in the evening, from 18:00 to 23:00, while the new entrants have the whole day to carry out the same obligation.

Instead of choosing one of the channels in our sample, viewers can select the outside option (corresponding to group 0) which consists of either watching one of the remaining free or pay TV channels (for which we have no individual data due to their very small audience) or engaging in activities other than watching TV.

The nested logit model allows for the incumbent TV channels to be considered as closer substitutes for each other than for the new channels. It also allows for the probability that a representative viewer chooses an incumbent channel to be higher than the probability of choosing a new channel, which is consistent with their respective audience shares and with the higher reputation and quality of incumbent channels compared to the new channels.

Formally, in each period t, the indirect utility of consumer i from watching channel j, belonging to the group g (incumbent, entrant or outside good), is given by:

$$U_{jgt}^{i} = \delta_{jt} + \zeta_{jgt}^{i}, \tag{1}$$

where δ_{jt} denotes the mean utility level of TV viewers from watching channel j or choosing the outside good at time t and ζ_{jgt}^i denotes the departure of consumer i's preference from the common utility level.¹⁴ We define:

$$\delta_{jt} = q_{jt} + \alpha A_{jt},\tag{2}$$

where q_{jt} denotes the perceived quality of channel j in period t and A_{jt} denotes the amount of advertising. We model the quality by $q_{jt} = X_{jt}\beta + \xi_{jt}$, where ξ_{jt} is a random term capturing the unobserved quality of channel j in period t and X_{jt} is a matrix of variables including observed content characteristics, channel-fixed effects, as well as month- and year-fixed effects. The observed content characteristics are broadcasting hours of TV series/movies, entertainment, news, culture/science, sports and cartoons, capturing the observable channel-time specific broadcasting quality. Channel dummies capture the brand awareness of each individual TV station; year dummies capture the potential changes in policy, fluctuations of the economic climate and the generalization of the digital TV technology; month dummies capture the seasonality of TV viewing.

We also specify the error term ζ_{jgt}^i in Equation (1), which reflects individual deviations from the mean valuation, as a weighted sum of two unobserved variables ε_{qt}^i and ε_{jt}^i given by:

$$\zeta_{jgt}^{i} = \varepsilon_{gt}^{i} + (1 - \sigma)\varepsilon_{jt}^{i}.$$
(3)

The term ε_{gt}^i affects the individual *i*'s preferences common to all channels belonging to group g, and the term $(1 - \sigma)\varepsilon_{jt}^i$ affects the individual *i*'s preferences specific to channel j. The two terms ε_{gt}^i and ε_{jt}^i are distributed in such a way that the individual preferences have an extreme value distribution and are allowed to be correlated across channels j. (See MacFadden *et al.*, 1978 and Williams, 1977.)

The parameters of interest to be estimated are α and σ . The parameter α denotes the mean preference of TV viewers for advertising: A positive (negative) value of α suggests that viewers value (disvalue, respectively) advertisements. We let the data decide the sign of α at the estimation stage. Moreover, a statistically significant α would confirm the two-sided nature of the TV market and is hence a crucial element of our structural estimation.

¹⁴Recall that we observe the monthly average number of viewers per channel per second, computed from the per second measurement by Médiamétrie. (See footnote 7.) We assume that a viewer chooses one channel to watch in a given second, but we only observe the average number of viewers per second for each channel in a given month.

The parameter $\sigma \in [0, 1)$ defines the substitutability of TV channels belonging to the same group. As σ approaches one, the TV viewers substitute significantly between channels within the same group g; as σ decreases, the correlation of preferences for channels within the same group decreases. Typically, $\sigma = 0$ signifies that the TV viewers are equally likely to switch between channels of different categories as between channels in the same group.

Following Berry (1994), the mean utility level for the outside good is normalized to 0, i.e., $\delta_0 = 0$, and the demand of viewers is specified as:

$$ln(\mathfrak{s}_{jt}) = X_{jt}\beta + \alpha A_{jt} + \sigma ln(\mathfrak{s}_{jt/q}) + ln(\mathfrak{s}_{0t}) + \xi_{jt}, \tag{4}$$

where \mathfrak{s}_{jt} (respectively, \mathfrak{s}_{0t}) is the probability that an individual chooses to watch channel j (respectively, to take the outside option) at time t. The probability \mathfrak{s}_{jt} is decomposed as the product of two probabilities: the probability $\mathfrak{s}_{jt/g}$ of watching channel j given that channel j belongs to group g and the probability \mathfrak{s}_{gt} that an individual chooses to watch channels of group g. The difference in brand awareness between incumbents and new entrants implies that the probability of choosing a new entrant. As we pass over the representative TV viewers, the choice probabilities \mathfrak{s}_{jt} , $\mathfrak{s}_{jt/g}$, \mathfrak{s}_{0t} coincide at the aggregate level with the market share of channel j s_{jt} , the market share of channel j within its group $s_{jt/g}$ and the market shares of the outside goods s_{0t} , respectively.

If T_t is the market size at time t, and if y_{jt} is the number of TV viewers watching channel j, the audience share of channel j and its audience share within its group are given by: $s_{jt} = y_{jt}/T_t$ and $s_{jt|g} = s_{jt} / \sum_{j \in C_g} s_{jt}$, respectively. The audience share of the outside good is obtained as $s_{0t} = 1 - \sum_j s_{jt}$.¹⁵

From Equation (4), we write the number of viewers as $y_{jt} = s_{jt}T_t \equiv y_{jt}(\mathbf{A}_t)$, where $\mathbf{A}_t = \{A_{1t}, \ldots, A_{jt}, \ldots, A_{Jt}\}$ is the vector of amounts of advertising for each channel. Then, the TV viewers' demand function to be estimated is given by:

$$\ln s_{jt} - \ln s_{0t} = \alpha A_{jt} + \sigma \ln s_{jt/q} + X_{jt}\beta + \xi_{jt}.$$
(5)

Identification

Equation (5) entails two identification problems. One concerns the parameter σ . Conceptually, observing the viewers' switching between channels within the same group (i.e., incumbent, entrant, or outside channels) over time should allow identifying σ , as it involves changes in the conditional probabilities of choosing the same group. These variations can be either the result of changes in the channels' characteristics or the result of changes in the number of channels operating in the market. There is, however, a potential endogeneity problem if viewers switch from a channel because of some unobserved changes in the characteristics of the TV channel. In Equation (5), when ξ_{jt} is high, the market share s_{jt} is high, but the conditional market share, $\bar{s}_{jt/g}$, is also high, not only because of viewers' switching from channels of the same group but also because of some viewers that have switched from channels of other categories. For instance, when an incumbent TV channel *j* increases the quality of its broadcasting content during period *t*, it attracts additional viewers both from other incumbent channels and from the new channels. We do not observe this change in the quality of channel *j*, which is captured by ξ_{jt} ; however, we observe an increase in its market share s_{jt} and its conditional market share $s_{jt/g}$. As a consequence, the estimate of σ could be biased upwards unless $s_{jt/g}$ is properly instrumented for.

Another issue of identification comes from the fact that the market shares of TV channels s_{jt} and the amounts of advertising A_{jt} are determined simultaneously. The random term ξ_{jt} includes

¹⁵In the empirical part, the market size T_t is considered to be the total population of France.

characteristics of channel j during period t that are unobserved by econometricians but are likely to be observed by the TV stations. The equilibrium level of advertising A_{jt} should be high (or low) if the TV operator anticipates that its viewership s_{jt} will be high (or low). Hence, without controlling for the A_{jt} , the estimate of α would be biased upward (or downward, respectively).

We use the following BLP-style instrumental variables to address the endogeneity issue: monthly broadcasting hours of news and entertainment of all competing channels, as well as monthly broadcasting hours of news and entertainment of all competing channels in a group (incumbent or entrant). Note that the channels which share a common ownership with the instrumented channel are not considered as competing channels in our IV construction. The validity of the above instruments relies on the timing of the decision about the broadcasting content and about the amount of advertising. According to experts in the industry, the broadcast TV content is decided about three months before the broadcasting time. Since the content is chosen simultaneously on different TV channels, the choice of a channel cannot depend on the content quality of a competing channel during the same period. In other words, the instrumental variables, i.e., the broadcasting hours of news and entertainment of competing channels within the same month, are independent of the error term, namely, the unobserved quality of the shows of the instrumented TV channel in Equation (5). Moreover, TV stations communicate their broadcasting content to the public about two months prior to their actual broadcasting time. The ASHs collect this information, and determine the optimal amount of advertising of each channel according to the attractiveness of its content with respect to the content of its competitors. Therefore, the instrumental variables, the broadcasting hours of different TV shows of competing channels, are correlated with the endogenous variable, namely, the amount of advertising of the instrumented channel A_{it} . The TV shows of the competing channels in a group (incumbent or entrant) can explain the conditional market shares of each channel in its respective group $s_{jt/g}$, meaning that this set of instruments, i.e., the broadcasting hours of different TV shows of competing channels in a group, is correlated with the endogenous variable, namely, the conditional market shares of each channel in its respective group $s_{jt/g}$.

3.2 Advertisers' demand

The literature on two-sided media markets has modelled advertisers' demand by their inverse demand curve relating the price of advertising to the amount of advertising and size of the audience. (See, among others, Rysman, 2004; Argentesi and Filistrucchi, 2007; Wilbur, 2008; Fan, 2013; Berry, Eizenberg, and Waldfogel, 2016.) While this approach can obtain the inverse demand elasticities of advertisers, it does not explicitly model the substitutability or complementarity between the advertising slots of different TV channels. Since cross-substitution of channels by advertisers can incentivize the ASHs to increase advertising prices via a merger, ignoring the substitutability and/or complementarity between the advertising slots of the TV channels could bias the results of the merger analysis that we carry out below. We propose a demand model which takes into account the advertisers' multi-homing behavior and allows us to estimate, from the aggregated advertising data, the cross-elasticities between the advertising slots of different TV channels.

To reach a wide range of TV viewers, advertisers place the same advertisements on different TV channels. The advertisers book the amount of advertising A_{jt} and require from the ASHs a minimum number of viewers y_{jt} . This activity comes at a cost. Let p_{jt} denote the price per second of advertising that the ASHs charge to advertisers. A representative advertiser's problem consists of choosing the vector of amounts of advertising $\mathbf{A}_t = (A_{1t}, ..., A_{Jt})$ that minimizes the total costs C_t of achieving the desired overall reach of audience, $Y_t = \sum_{j}^{J} y_{jt}$. The associated cost function of

the advertiser is defined as:

$$C_t = C(\mathbf{p_t}, Y_t) = \left\{ \min_{A_{1t}, \dots, A_{Jt}} \sum_j p_{jt} \times A_{jt} | \mathcal{F}(A_{1t}, \dots, A_{Jt}) \le Y_t \right\},\tag{6}$$

where $\mathbf{p_t} = (p_{1t}, ..., p_{Jt})$ and $\mathcal{F}(A_{1t}, ..., A_{Jt}) \leq Y_t$ is the production function of the representative advertiser.

We assume that this cost function can be approximated by a translog flexible form as:¹⁶

$$\ln C_{t} = \gamma_{0} + \gamma_{y} \ln Y_{t} + \frac{1}{2} \gamma_{yy} (\ln Y_{t})^{2} + \sum_{j}^{J} \gamma_{j} \ln p_{jt} + \frac{1}{2} \sum_{i}^{J} \sum_{j}^{J} \gamma_{ij} (\ln p_{it}) (\ln p_{jt}) + \sum_{j}^{J} \theta_{j} (\ln Y_{t}) (\ln p_{jt}) + \sum_{j}^{J} \xi_{jt}^{A} \ln p_{jt},$$
(7)

where ξ_{jt}^A denotes the error term. Taking the derivative of Equation (7) with respect to $\ln p_{jt}$ and applying Shephard's lemma yields the cost share equations for each TV channel j:¹⁷

$$S_{jt}^{A} = \gamma_j + \sum_{i}^{J} \gamma_{ij}(\ln p_{it}) + \theta_j(\ln Y_t) + \xi_{jt}^{A}$$

$$\tag{8}$$

To satisfy the adding-up, homogeneity and symmetry conditions of the duality theory, the parameters of the translog cost function must satisfy the following constraints:¹⁸

$$\sum_{j}^{J} \gamma_{j} = 1 \quad \text{and} \quad \sum_{j}^{J} \gamma_{ij} = \sum_{i}^{J} \gamma_{ij} = \sum_{j}^{J} \theta_{j} = 0 \quad \text{and} \quad \gamma_{ij} = \gamma_{ji}$$
(9)

Solving the system of Equations (8) yields the vector of advertising prices $p_{jt} \equiv p_{jt}(\mathbf{A}_t, Y_t)$. The own- and cross-price elasticities of the advertiser's demand $(E^A_{jj,t}, E^A_{ji,t})$ can be derived from the Allen partial elasticities of substitution (see Berndt and Wood, 1975):

$$E_{jj,t}^{A} = \frac{\partial A_{j,t} p_{j,t}}{\partial p_{j,t} A_{j,t}} = \gamma_{jj} / S_{j,t}^{A} + S_{j,t}^{A} - 1$$
(10)

$$E_{ji,t}^{A} = \frac{\partial A_{j,t} p_{i,t}}{\partial p_{i,t} A_{j,t}} = \gamma_{ij} / S_{j,t}^{A} + S_{i,t}^{A}$$
(11)

Identification

We estimate the system of advertising cost share equations, specified by Equations (8), under the constraints in Equations (9), using Zellner's iterated seemingly unrelated regression method. To avoid the singularity of the covariance matrix of the advertising cost share system, one share

¹⁶The translog cost function is flexible in the sense that it does not impose restrictions on the substitutability or complementarity between the input factors $(A_{it} \text{ and } A_{jt}, \forall i \neq j)$. (See Berndt, 1991; Christensen *et al.*, 1973.) ${}^{17}S_{jt}^{A} = \frac{\partial \ln C_t}{\partial \ln p_{jt}} = \frac{p_{jt}\partial C_t}{C_t \partial p_{jt}} = \frac{p_{jt}A_{jt}}{C_t}$.

¹⁸Since each cost share is the proportion of the total advertising cost spent on that input, the cost shares of the different TV stations must sum to one. This condition implies that the intercepts of the cost share equations must sum to one, while both the row and column coefficients must sum to zero. In addition, imposing the symmetry $\gamma_{ij} = \gamma_{ji}$ guarantees the integrability of the demand function of the advertisers. (See Hurwicz and Uzawa, 1971.)

equation must be omitted in the estimation. We select randomly one channel, channel j, to omit, but recover its parameters, γ_j , γ_{ij} and θ_j , using the restrictions given by Equations (9).

The error term ξ_{jt}^A may include the broadcasting quality of channel j in month t, which has an impact on both A_{jt} and $p_{1t}, ..., p_{Jt}$. If this is the case, there would be a problem of endogeneity. We then need instruments for $\ln p_{1t}, ..., \ln p_{Jt}$ to estimate the system of advertising cost share equations using the three-stage least squares method. We have compared two sets of instruments for $p_{1t}, ..., p_{Jt}$: the twice-lagged logarithm of the price of advertising (i.e., $\ln p_{1t-2}, ..., \ln p_{Jt-2}$) and the broadcasting hours of news and entertainment programs of the competing channels (also used as instruments for A_{jt} in the viewers' demand model).^{19,20} For each set of instruments, we tested the difference between the estimates with and without instrumenting for $\ln p_{jt}$ using the Hausman test. The testing results do not reject the null assumption that the difference between the estimates under the two specifications (with and without IVs) is not systematic. In other words, we obtain very similar estimates with and without instrumenting for $\ln p_{jt}$; thus $\ln p_{jt}$ can be treated as exogenous in Equations (8).

4 Estimation results

4.1 Viewers' demand

The estimation results for Equation (5) are presented in Table 5. Both the coefficient associated with the amount of advertising, $\hat{\alpha}$, and the one associated with the within-nest shares, $\hat{\sigma}$, are significant at the one percent level. Since $\hat{\alpha} < 0$, an increase in the amount of advertising induces a decrease in the number of viewers of the TV channel. This result suggests that, on average, TV viewers are adversely sensitive to the amount of advertising. The estimated $\hat{\sigma}$ is significantly smaller than 1, indicating that there is competition between the incumbents and the new channels, although its value suggests that there is significant segmentation between the two groups of TV channels (incumbents and entrants).

Note that news and cartoons have a statistically significant mean positive effect on the size of the audience, but entertainment has a statistically significant mean negative effect on the size of the audience. This latter fact, which looks counterintuitive, can be explained as follows: The entertainment genre includes many unpopular programs that the TV channels use to fill the broadcasting slots during working hours and sleeping time; several high-quality shows belonging to this category are exclusively broadcast by the incumbent channels; their impact on audience size is captured by the nest parameter and the channel fixed effect. We could not identify any statistically significant effect of either TV series/movies or culture/science on the audience size, because the total broadcasting hours of both genres do not vary from one month to another, although their availability (in terms of broadcasting hours) is very channel specific. In other words, the effects of TV series/movies and culture/science programs on the audience size of a TV channel are absorbed

¹⁹The validity of these two sets of instruments relies on the timing of the decisions about advertising prices and broadcasting content. A key institutional detail is that the advertising prices $p_{1t}, ..., p_{Jt}$ are fixed about one month after the broadcasting content ξ_{jt}^A , while the ASHs and advertisers should not have any information about ξ_{jt}^A three months before the broadcasting time. First, the twice-lagged prices $p_{1t-2}, ..., p_{Jt-2}$ are independent of the error term ξ_{jt}^A , as the $p_{1t-2}, ..., p_{Jt-2}$ are fixed prior to the revelation of ξ_{jt}^A ; the twice-lagged prices $p_{1t-2}, ..., p_{Jt-2}$ are likely to be correlated with the endogenous variables $p_{1t}, ..., p_{Jt}$, as the same advertisements are often repeated for several months on the same channel. Second, as the content is chosen simultaneously by the different TV channels, the broadcasting quality of channel j cannot depend on the quality of the content of the other competing channels during the same period t (in other words, the error term ξ_{jt}^A is independent of the second set of IVs); the advertising prices are fixed about one month after the broadcasting content, which implies that the endogenous variables $p_{1t}, ..., p_{Jt}$

²⁰The first stage estimations with each set of IVs are provided in Table A6 and Table A7 in Appendix A.

by the channel fixed effect in the monthly data. We have identified a positive effect of sports on the audience size, although the parameter is not significant at usual levels. This is because there is an important heterogeneity between the different sport events: This genre includes the broadcasting of the Champions League, the Roland Garros tennis tournament, and the Olympic Games, but also many small sports events that are scheduled daily between 00:00 and 06:00. We note here that monthly data are not the best way to study the effects of genre on audience size. TV channels have a strategy of scheduling different genres at different times of day, but the availability of many genres (in terms of broadcasting hours) does not vary significantly from one month to another. However, the broadcasting hours of different program genres are here covariates that we control for in the viewers' demand model to better identify the disutility of advertising (measured by $\hat{\alpha}$) and the segmentation between the incumbent channels and the new entrants (measured by $\hat{\sigma}$).²¹

	$\ln s_{jt} - \ln s_{0t}$	
	coeff.	(s.e.)
Amount of advertising (α)	-0.111***	(0.031)
Within-nest share (σ)	0.636^{***}	(0.192)
${ m TV}~{ m Series}/{ m Movies}$	0.003	(0.003)
$\operatorname{Culture}/\operatorname{Science}$	0.001	(0.004)
News	0.068***	(0.009)
Entertainment	-0.255***	(0.078)
Sports	0.011	(0.009)
Cartoons	0.461^{**}	(0.111)
Channel FE	Yes	
Month FE	Yes	
Year FE	Yes	
No. observations	840	
Cragg–Donald Wald F statistic	14.665	
Hansen J statistic (p -value)	0.440	

Table 5: Estimates of viewers' demand

Note: Standard errors are in parentheses: ***p < 0.01, **p < 0.05, *p < 0.1

To validate our choice of instruments, we conducted statistical tests for weak instruments and overidentification of the IV estimations of Equation (5). The results are presented in the bottom of Table 5. The Stock–Yogo weak instrument test suggests the instruments are strong, while the Hansen J statistic does not reject the null hypothesis that the instruments are valid at the 10 percent level.

The first stage regressions are presented in Table A3 in Appendix A. The total number of hours of news and entertainment broadcast by all the competing channels can explain the amount of advertising on the instrumented channel. News has a mean positive effect on the size of the audience, while entertainment programs have a mean negative effect on the size of the audience.

 $^{^{21}}$ Zhang (2019) provides more detailed comments and more precise estimation of the different genre effects on the audience size of a TV channel using hourly data.

(See Table 5.) Accordingly, the amount of advertising of competing channels is higher during news programs, but lower during entertainment programs. The amount of advertising of the instrumented channel is higher when it anticipates more advertising by its rivals, due to their scheduling of more news and/or less entertainment programs. The sum of the broadcasting hours of news and entertainment programs of the competing channels in a group (incumbent, entrant) significantly explain the logarithm of the conditional market share, $\ln(s_{jt/g})$. The conditional market share of a channel decreases with the amount of news broadcast by its close competitors (i.e., competing channels in the same group), but increases with the amount of entertainment broadcast by its close competitors. We have also tested whether the estimates in Table 5 are robust to the choice of instruments, by including additional instrumental variables in the estimation. Such an experiment does not change significantly the values of the estimates but decreases the associated Cragg-Donald Wald F statistics. (See Table A5 in Appendix A for details.)

To determine whether the instruments used in the estimation are helpful in fixing the endogeneity bias, we compare the results from the IV estimation with those from OLS in Table A4 in Appendix A. We observe that the parameter estimates associated with the amount of advertising and the within-nest share in the viewers' demand function strongly differ under the two types of estimation. Without controlling for the endogeneity bias, the quantity of advertising reflects the quality of TV channel and is estimated to have a positive effect on the audience of the channel. The effect of the disutility of advertising can be isolated from the effect of the quality of the TV channel only if the endogeneity bias is properly controlled for. Moreover, with the nested-logit model specification, the value of $\hat{\sigma}$ should be between 0 and 1. This constraint is not satisfied with OLS.

The own- and cross-elasticities of the viewers' demand with respect to the amount of advertising $(E_{jj,t}^V, E_{ji,t}^V)$ follow the classical formula in the nested-logit model. (See, for instance, Verboven, 1996.) Their estimates, averaged by channel over the sample periods, are presented in Table 6. they suggest a median audience loss of about 8.7 percent in response to a 10 percent increase in advertising time.²² All the estimates of own-demand elasticities are significant at the 10 percent significance level. The estimated cross-demand elasticities are very small, suggesting that viewers substitute between channels to a very limited degree. Nevertheless, it is important to note that viewers do switch to other channels following an increase in the amount of advertising, although the estimated substitution effects are very small. This is true notably for channels TF1, NT1 and TMC, which suggests that these three channels do have an incentive to merge their ASHs in order to internalize the competition between them for the audience. However, given the weak substitution effects of advertising, we should not expect an important change in the amount of advertising following the merger of their ASHs.

4.2 Advertisers' demand

The estimates of γ_{ij} in the cost share Equations (8) are presented in Table 7. All the estimates of γ_{jj} , $\forall j$ are positive and statistically significant.²³ Many of the γ_{ij} , $i \neq j$ are estimated to be close to zero.

 $^{^{22}}$ We find relatively small own-demand elasticities, compared to previous articles using US data. Wilbur (2008) finds that a 10 percent rise in advertising time causes a median 25 percent audience loss for highly rated TV networks, and larger percentage audience losses for low-rated networks. Using improved audience measurement, Wilbur, Goeree and Ridder (2009) find a median audience loss of about 15 percent in response to a 10 percent increase in advertising time. The difference between our estimates and the findings in Wilbur *et al.* (2009) could be explained by the much more intensive TV advertising in the US.

²³Note that a positive sign of γ_{jj} does not imply positive demand elasticity. (See Equations (10) and (11) in Section 3.2.)

		E_{jj}^V	E_{ji}^V _SG	E_{ji}^V _DG
Incumbents	$\mathrm{TF1}$	-0.120	0.0033	0.00085
		(0.074)	(0.0023)	(0.00024)
	FR2	-0.062	0.0011	0.00020
		(0.038)	(0.0008)	(0.00008)
	$\mathrm{FR3}$	-0.054	0.0006	0.00017
		(0.033)	(0.0004)	(0.00005)
	M6	-0.108	0.0013	0.00033
		(0.066)	(0.0009)	(0.00009)
	$\mathbf{FR5}$	-0.036	0.0001	0.00003
		(0.022)	(0.0001)	(0.00001)
3	3.707.1	0.115	0.0000	0.00000
New entrants	NT1	-0.117	0.0008	0.00006
		(0.072)	(0.0007)	(0.00002)
	TMC	-0.118	0.0015	0.00011
		(0.072)	(0.0013)	(0.00003)
	D8	-0.101	0.0008	0.00006
		(0.062)	(0.0007)	(0.00002)
	FR4	-0.041	0.0003	0.00002
		(0.025)	(0.0002)	(0.00001)
	Gulli	-0.061	0.0005	0.00003
		(0.038)	(0.0004)	(0.00001)
	D17	-0.080	0.0003	0.00002
		(0.050)	(0.0003)	(0.00001)
	W9		0.0014	· · · · · ·
Notes EV CC d	W9	-0.097 (0.060)	$0.0014 \\ (0.0012)$	(0.00001) 0.00008 (0.00002)

Table 6: Viewers' demand elasticities with respect to the amount of advertising

Note: E_{ji}^V _SG denotes the cross-elasticities between channels within the same group (incumbents and entrants); E_{ji}^V _DG denotes the cross-elasticities between channels of two different groups (incumbents and entrants). Standard errors computed by delta method are in parentheses.

	S^A_{TF1}	S^A_{FR2}	S^A_{FR3}	S^A_{M6}	S^A_{FR5}	S^A_{D8}	S^A_{NT1}	S^A_{FR4}	S^A_{TMC}	S^A_{Gulli}	S^A_{D17}	S^A_{W9}
$\ln p_{TF1}$	$0.107 \\ (0.02)$	-0.023 (0.01)	-0.009 (0.01)	$\begin{array}{c} 0.025 \\ (0.02) \end{array}$	-0.002 (0.00)	-0.016 (0.01)	-0.014 (0.00)	-0.003 (0.00)	-0.024 (0.01)	-0.014 (0.01)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	-0.029 (0.01)
$\ln p_{FR2}$	-0.023 (0.01)	$\begin{array}{c} 0.036 \\ (0.00) \end{array}$	$\begin{array}{c} 0.002 \\ (0.00) \end{array}$	$\begin{array}{c} 0.012 \\ (0.01) \end{array}$	$0.000 \\ (0.00)$	-0.008 (0.00)	-0.010 (0.00)	-0.004 (0.00)	-0.004 (0.00)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	-0.003 (0.07)
$\ln p_{FR3}$	-0.009 (0.01)	$\begin{array}{c} 0.002 \\ (0.00) \end{array}$	$\begin{array}{c} 0.025 \\ (0.00) \end{array}$	-0.012 (0.01)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	-0.002 (0.00)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	$\begin{array}{c} 0.004 \\ (0.00) \end{array}$	-0.014 (0.00)	$0.006 \\ (0.00)$	$\begin{array}{c} 0.003 \\ (0.00) \end{array}$	-0.005 (0.00)
$\ln p_{M6}$	$\begin{array}{c} 0.025 \\ (0.02) \end{array}$	$\begin{array}{c} 0.012 \\ (0.01) \end{array}$	-0.012 (0.01)	$\begin{array}{c} 0.064 \\ (0.02) \end{array}$	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	$\begin{array}{c} 0.001 \\ (0.01) \end{array}$	-0.001 (0.00)	$\begin{array}{c} 0.003 \\ (0.00) \end{array}$	$\begin{array}{c} 0.008 \\ (0.01) \end{array}$	-0.024 (0.01)	-0.009 (0.00)	-0.010 (0.01)
$\ln p_{FR5}$	-0.002 (0.00)	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	$\begin{array}{c} 0.004 \\ (0.00) \end{array}$	-0.001 (0.00)	-0.000 (0.00)	-0.001 (0.00)	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	-0.002 (0.00)
$\ln p_{D8}$	-0.016 (0.01)	-0.008 (0.00)	-0.002 (0.00)	$\begin{array}{c} 0.001 \\ (0.01) \end{array}$	-0.001 (0.00)	$\begin{array}{c} 0.018 \\ (0.00) \end{array}$	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	-0.003 (0.00)	-0.005 (0.01)	$\begin{array}{c} 0.007 \\ (0.00) \end{array}$	$0.008 \\ (0.00)$
$\ln p_{NT1}$	-0.014 (0.01)	-0.010 (0.00)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	-0.001 (0.00)	-0.000 (0.00)	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	$\begin{array}{c} 0.037 \\ (0.00) \end{array}$	-0.000 (0.00)	$\begin{array}{c} 0.003 \\ (0.01) \end{array}$	-0.004 (0.00)	-0.007 (0.00)	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$
$\ln p_{FR4}$	-0.003 (0.00)	-0.004 (0.00)	$\begin{array}{c} 0.004 \\ (0.00) \end{array}$	$\begin{array}{c} 0.003 \\ (0.00) \end{array}$	-0.001 (0.00)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	-0.000 (0.00)	$\begin{array}{c} 0.003 \\ (0.00) \end{array}$	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	-0.003 (0.00)	-0.001 (0.00)	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$
$\ln p_{TMC}$	-0.024 (0.01)	-0.004 (0.00)	-0.014 (0.00)	$\begin{array}{c} 0.008 \\ (0.01) \end{array}$	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	-0.003 (0.00)	$\begin{array}{c} 0.003 \\ (0.01) \end{array}$	$\begin{array}{c} 0.000 \\ (0.00) \end{array}$	$\begin{array}{c} 0.042 \\ (0.00) \end{array}$	-0.005 (0.00)	-0.006 (0.01)	$\begin{array}{c} 0.008 \\ (0.00) \end{array}$
$\ln p_{Gulli}$	-0.014 (0.01)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	$0.006 \\ (0.00)$	-0.024 (0.01)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	-0.005 (0.01)	-0.004 (0.01)	-0.003 (0.00)	-0.005 (0.00)	$\begin{array}{c} 0.057 \\ (0.01) \end{array}$	-0.003 (0.02)	-0.007 (0.00)
$\ln p_{D17}$	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	$\begin{array}{c} 0.003 \\ (0.00) \end{array}$	-0.009 (0.00)	$\begin{array}{c} 0.001 \\ (0.00) \end{array}$	$\begin{array}{c} 0.007 \\ (0.01) \end{array}$	-0.007 (0.01)	-0.001 (0.01)	-0.006 (0.01)	-0.003 (0.02)	$\begin{array}{c} 0.019 \\ (0.02) \end{array}$	-0.007 (0.00)
$\ln p_{W9}$	-0.029 (0.01)	-0.003 (0.07)	-0.005 (0.00)	-0.010 (0.01)	-0.002 (0.00)	$0.008 \\ (0.00)$	$0.000 \\ (0.00)$	$0.000 \\ (0.00)$	$0.008 \\ (0.00)$	-0.007 (0.00)	-0.007 (0.00)	$\begin{array}{c} 0.047 \\ (0.00) \end{array}$
$\ln Y$	$0.836 \\ (0.25)$	-0.031 (0.07)	-0.079 (0.05)	-0.089 (0.16)	-0.029 (0.01)	-0.171 (0.07)	-0.068 (0.03)	-0.011 (0.01)	-0.075 (0.05)	-0.235 (0.13)	$0.046 \\ (0.04)$	-0.090 (0.09)
				Nu	mber of	observati	ons per e	equation:	69			

Table 7: Cost share input price coefficient estimates

Note: Standard errors of estimates are in parentheses.

Using these estimates, we compute the own- and cross-price elasticities of advertisers' demand for viewers $(E_{jj,t}^A \text{ and } E_{ji,t}^A)$ according to Equations (10) and (11). The estimates by channel, averaged over the period of observation, are presented in Table 8. Each cell of this table displays the percentage change in demand that the row channel benefits from the column channel's change in its price by one percent. The estimates of own-price elasticities are statistically significant for all channels. These results suggest that advertisers' demand for viewers is relatively price inelastic since all cross-price elasticities are smaller than one in absolute value.

Inter-channel substitutability coexists with complementarity. Out of the 132 average cross-

	1											
	TF1	FR2	FR3	M6	FR5	D8	NT1	FR4	TMC	Gulli	D17	W9
TF1	-0.30 (0.05)	$\begin{array}{c} 0.00\\ (0.02) \end{array}$	$0.01 \\ (0.01)$	0.28 (0.04)	$\begin{array}{c} 0.00 \\ (0.00) \end{array}$	-0.00 (0.01)	-0.04 (0.01)	-0.00 (0.00)	-0.06 (0.01)	-0.01 (0.01)	$0.02 \\ (0.01)$	-0.01 (0.01)
FR2	-0.02 (0.16)	-0.21 (0.10)	$0.06 \\ (0.07)$	$\begin{array}{c} 0.46 \\ (0.16) \end{array}$	$\begin{array}{c} 0.01 \\ (0.02) \end{array}$	-0.14 (0.05)	-0.17 (0.04)	-0.07 (0.01)	-0.04 (0.07)	$\begin{array}{c} 0.05 \\ (0.07) \end{array}$	$\begin{array}{c} 0.04 \\ (0.05) \end{array}$	-0.02 (0.07)
FR3	$ \begin{array}{c} 0.20 \\ (0.22) \end{array} $	$\begin{array}{c} 0.10 \\ (0.12) \end{array}$	$-0.18 \\ (0.10)$	-0.16 (0.20)	$\begin{array}{c} 0.02 \\ (0.03) \end{array}$	-0.04 (0.07)	$0.06 \\ (0.06)$	$\begin{array}{c} 0.13 \\ (0.02) \end{array}$	-0.38 (0.10)	$\begin{array}{c} 0.21 \\ (0.08) \end{array}$	$\begin{array}{c} 0.12 \\ (0.07) \end{array}$	-0.10 (0.09)
M6	$\begin{array}{c} 0.59 \\ (0.08) \end{array}$	$\begin{array}{c} 0.10 \\ (0.04) \end{array}$	-0.02 (0.03)	$-0.75 \ (0.10)$	$\begin{array}{c} 0.01 \\ (0.01) \end{array}$	$\begin{array}{c} 0.04 \\ (0.02) \end{array}$	$\begin{array}{c} 0.02 \\ (0.02) \end{array}$	$\begin{array}{c} 0.02 \\ (0.01) \end{array}$	$\begin{array}{c} 0.09 \\ (0.03) \end{array}$	-0.08 (0.03)	-0.02 (0.02)	$0.00 \\ (0.03)$
FR5	$ \begin{array}{c} 0.07 \\ (0.22) \end{array} $	$\begin{array}{c} 0.11 \\ (0.15) \end{array}$	$\begin{array}{c} 0.17 \\ (0.14) \end{array}$	$\begin{array}{c} 0.29 \\ (0.22) \end{array}$	-0.33 (0.10)	-0.21 (0.07)	-0.02 (0.12)	-0.10 (0.03)	$\begin{array}{c} 0.05 \\ (0.15) \end{array}$	$\begin{array}{c} 0.13 \\ (0.08) \end{array}$	$\begin{array}{c} 0.13 \\ (0.09) \end{array}$	-0.26 (0.11)
D8	-0.05 (0.17)	-0.23 (0.09)	-0.04 (0.07)	$\begin{array}{c} 0.27 \\ (0.17) \end{array}$	-0.04 (0.01)	-0.37 (0.07)	$0.04 \\ (0.04)$	$\begin{array}{c} 0.03 \\ (0.01) \end{array}$	-0.04 (0.06)	-0.13 (0.08)	$\begin{array}{c} 0.25 \\ (0.05) \end{array}$	$0.30 \\ (0.07)$
NT1	-0.35 (0.12)	-0.28 (0.06)	$\begin{array}{c} 0.06 \\ (0.07) \end{array}$	$\begin{array}{c} 0.19 \\ (0.12) \end{array}$	-0.00 (0.02)	$0.04 \\ (0.04)$	$-0.29 \ (0.07)$	$\begin{array}{c} 0.00 \\ (0.02) \end{array}$	$\begin{array}{c} 0.31 \\ (0.08) \end{array}$	-0.12 (0.05)	-0.21 (0.05)	$0.05 \\ (0.06)$
FR4	-0.16 (0.27)	-0.65 (0.13)	$\begin{array}{c} 0.83 \\ (0.13) \end{array}$	$\begin{array}{c} 0.83 \\ (0.26) \end{array}$	-0.11 (0.03)	$\begin{array}{c} 0.20 \\ (0.08) \end{array}$	$\begin{array}{c} 0.02 \\ (0.09) \end{array}$	-0.47 (0.04)	$\begin{array}{c} 0.10 \\ (0.14) \end{array}$	-0.54 (0.10)	-0.14 (0.09)	0.07 (0.13)
TMC	-0.49 (0.13)	-0.04 (0.07)	-0.24 (0.06)	$\begin{array}{c} 0.39 \\ (0.13) \end{array}$	$\begin{array}{c} 0.01 \\ (0.02) \end{array}$	-0.03 (0.04)	$\begin{array}{c} 0.17 \\ (0.05) \end{array}$	$\begin{array}{c} 0.01 \\ (0.01) \end{array}$	$-0.09 \\ (0.03)$	-0.08 (0.05)	-0.10 (0.05)	0.21 (0.07)
Gulli	-0.11 (0.30)	$\begin{array}{c} 0.11 \\ (0.14) \end{array}$	$0.28 \\ (0.10)$	-0.77 (0.30)	$\begin{array}{c} 0.03 \\ (0.02) \end{array}$	-0.16 (0.10)	-0.14 (0.06)	-0.11 (0.02)	-0.16 (0.10)	-0.38 (0.22)	-0.09 (0.08)	-0.24 (0.13)
D17	$\begin{array}{c} 0.53 \\ (0.24) \end{array}$	$\begin{array}{c} 0.11 \\ (0.12) \end{array}$	$0.19 \\ (0.11)$	-0.22 (0.24)	$\begin{array}{c} 0.04 \\ (0.02) \end{array}$	$\begin{array}{c} 0.38 \\ (0.08) \end{array}$	-0.30 (0.07)	-0.03 (0.02)	-0.25 (0.11)	-0.11 (0.10)	$-0.06 \ (0.01)$	-0.30 (0.11)
W9	-0.10 (0.15)	-0.02 (0.07)	-0.06 (0.06)	0.02 (0.14)	-0.03 (0.01)	$\begin{array}{c} 0.19 \\ (0.05) \end{array}$	0.03 (0.04)	0.01 (0.01)	0.21 (0.07)	-0.12 (0.06)	-0.12 (0.05)	-0.05 (0.02)

Table 8: Own- and cross-price elasticities of advertisers' demand

Note: Standard errors computed by delta method are in parentheses. Own-price elasticities are in bold. Negative cross-price elasticities statistically significant at 10% are in italic.

price elasticities, 67 (i.e., 51 percent) indicate that channels are substitutes. However, the precision of the estimates tends to be greater for complements than for substitutes: While 60 percent of the negative average cross-price elasticities are statistically significant, this percentage drops to 48 percent for the positive average cross-price elasticities. The magnitude of cross-price effects, whether they identify substitutes or complements, tends to be limited. The median value of the 67 positive average cross-price elasticities is 0.07 (with a range between 8×10^{-4} and 0.83, with only one value that exceeds 1). The median value of the 62 negative cross-price elasticities is -0.11 (with a range between -0.77 and -3×10^{-3}).

We note that the advertisers consider channels NT1 and TMC as substitutes, but both as complements of channel TF1. This demand pattern of the advertisers suggests that a merger between the ASH of channel TF1 with the ASH of channels NT1 and TMC would not lead to a significant increase in their advertising prices. If the merged ASH increased the price of advertising

on channel TF1, the marginal advertisers would not switch to NT1 or TMC but to the other channels that are substitutes for channel TF1.

5 Merger evaluation

In January 2010, the Autorité de la concurrence (the French competition authority) cleared the acquisition of two free broadcast TV channels, NT1 and TMC, by the TF1 Group, subject to a behavioral remedy requiring that channels NT1 and TMC sell their advertising time separately from the main channel of TF1 Group, namely, channel TF1. In practice, the decision prohibits the merger between the ASH of channel TF1 and that of channels NT1 and TMC; only the broadcasting content of the three channels is allowed to be managed jointly following the acquisition.

The competition authority had concluded that the acquisition would have a positive impact on the broadcasting side, since channels NT1 and TMC could benefit from the large catalog of programs of TF1 Group (which is due to its partnership with numerous content providers): Having more channels offering high-quality content could enhance the competition between the different TV broadcasters for audience.²⁴

The authority was, however, concerned about the potential anti-competitive effects of merging the ASHs of the three channels, due to the dominant position of TF1 Group in the TV advertising market. Before the acquisition, the ASH of channel TF1 held a 40 percent market share, while the ASH of NT1 and TMC held a five percent market share. The merger could simply reinforce the position of TF1 Group in the advertising market, which would translate into an increase in either the amount of advertising or its price. To avoid any detrimental effect of the acquisition on the TV advertising market, the authority decided to impose this behavioral remedy for a period of at least five years.²⁵

Below, we first provide some reduced-form evidence on the impact of the acquisition on the TV advertising market. We next explain why it is crucial to account for the interaction between the two sides of the market by exploiting the strategic decisions of the ASHs. In more detail, we estimate the changes in broadcasting quality of the three merging channels from our viewers' demand model; then, we counterfactually simulate the effects of the acquisition in the absence of the two-sided network externalities between viewers and advertisers, to decompose the direct impact of the changes in broadcasting quality and the effect of two-sided network externalities on the amounts and prices of advertising by the merging channels. Finally, to comment on the effectiveness of the implemented remedy, we counterfactually simulate the advertising market equilibrium for the case in which the ASH of NT1 and TMC merged with the ASH of channel TF1 following the acquisition.

5.1 Evidence of the effects of the merger

To get an initial insight into the impact of the acquisition on the amounts and prices of advertising by the merging channels, we estimate the following regression, in line with Ashenfelter and Hosken (2010) and Björnerstedt and Verboven (2015):

$$\ln A_{jt} = \mu_j^1 + \mu_t^2 + \rho_j PostAcquisition_t + \eta_{jt};$$

$$\ln P_{jt} = \tau_j^1 + \tau_t^2 + \lambda_j PostAcquisition_t + \omega_{jt},$$

²⁴While NT1 and TMC are growing very fast as new entrants to the market, their catalogs of broadcasting programs are not as rich as the catalogs of the incumbent channels like TF1.

²⁵The ASHs of the three channels have remained separate after the effective period of the behavioral remedy, possibly because TF1 Group did not want to encourage increased scrutiny by the competition authority.

where A_{jt} denotes the amount of advertising by channel j and P_{jt} its price during period (monthyear) t; μ_j^1 and τ_j^1 denote the channel fixed effect; μ_t^2 and τ_t^2 denote the month-year time fixed effect; the variable *PostAcquisition*_t is equal to 0 from March 2008 to January 2010, and is equal to 1 from January 2010 to December 2013, for all channels.

As noted by Björnerstedt and Verboven (2015), these regressions can be interpreted as differencein-differences estimators, where the difference between the merging firms' ρ_j (or λ_j) and the competitors' ρ_j (λ_j) measures the effect of the acquisition on the amounts (prices, respectively) of advertising under the assumption that the acquisition does not have an impact on the competitors' amounts (prices) of advertising. In practice, however, the acquisition could raise the competitors' prices as well; then, the difference between the merging firms' ρ_j (λ_j) and the competitors' ρ_j (λ_j) could be viewed as a lower bound of the effect of the merger on the amount (price) of advertising of channel j.

We use our full sample (22 months' pre-acquisition data and 47 months' post-acquisition data) to estimate the channel-specific treatment effects ρ_j and λ_j . The estimation results are presented in Table 9.²⁶

	Amount of	advertising	Advertising	price
	(percent cha	ange)	(percent cha	ange)
	coeff .	(s.e.)	coeff.	(s.e.)
$TF1 \times Acquisition$	29.06^{***}	(0.099)	26.77***	(0.100)
$NT1 \times Acquisition$	49.71***	(0.115)	119.44^{***}	(0.174)
$TMC \times Acquisition$	43.761^{***}	(0.110)	110.60^{***}	(0.167)
$Others \times Acquisition$	Yes		Yes	
Channel FE	Yes		Yes	
Month-Year FE	Yes		Yes	

Table	9:	Effects	of	the	merger
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Note: The percentage effects on the amount of advertising and price are obtained from a transformation of the parameters ρ_j and λ_j using $\exp(\rho_j) - 1$ and $\exp(\lambda_j) - 1$. Standard errors are computed using the delta method. ***p < 0.01, **p < 0.05, *p < 0.1

Our results suggest that the acquisition led to a significant increase in both the amounts and prices of advertising by the three merging channels. We also notice that the acquisition affected the two purchased channels more strongly than channel TF1. These results could eventually be explained by the increase in broadcasting quality of the merging channels following the acquisition. Intuitively, viewers' demand is less elastic to the amount of advertising during better broadcasting content, which implies that the ASHs of the merging channels have an incentive to increase their amount of advertising following the acquisition as a strategic reaction to an increase in their broadcasting quality: Better programs attract more viewers, which in turn increases advertisers'

²⁶Since the acquisition was announced in January 2010, while the merger of broadcasting services of the three channels could have taken time, we also re-estimated ρ_j and λ_j , excluding the post-acquisition data immediately following the announcement of the acquisition (from February 2010 to December 2010), i.e., using 22 months' pre-acquisition data and 36 months' post-acquisition data, as a robustness check. The estimates using this reduced post-acquisition sample are presented in Table A8 in Appendix A. We obtain very similar results with the two samples.

willingness to pay for the advertising slots of these two channels. As we find a stronger affect of the acquisition on the two purchased channels than on channel TF1, we conjecture that the acquisition may have been followed by a reallocation of high-quality programs from channel TF1 to the two purchased channels NT1 and TMC. We estimate the post-acquisition changes in broadcasting quality of the three channels from our viewers' demand model in Section 5.3 below.

5.2 Market Equilibrium

We now write down the profit maximization problem of ASHs, which we use to perform different counterfactual simulations. The profit of an ASH depends on the demands of viewers and advertisers and on the feedback loop between the two groups of consumers. Each ASH maximizes the joint profit from the advertising slots of all the channels under its management. Formally, the profit function of an ASH $\mathscr{H}_k, k = \{1, ..., K\}$ in month t is given by:

$$\Pi_{kt} = \sum_{j \in \mathscr{H}_k} \Pi_{jt} = \sum_{j \in \mathscr{H}_k} \left(p_{jt} - c_{jt} \right) A_{jt},\tag{12}$$

where c_{jt} is the marginal cost of commercializing one second of advertising on channel j in month t for the ASH \mathscr{H}_k .

At equilibrium, the amount of advertising is the variable which links both sides of the market: It has an impact on both the number of viewers and on the advertising prices of the TV channels. An ASH internalizes the network externalities between viewers and advertisers by choosing the amount of advertising which maximizes its profits. Using the notation introduced in Section 3.1 where we write down the number of viewers y_{jt} of channel j as a function of the amounts of advertising of different TV channels \mathbf{A}_t : $y_{jt} \equiv y_{jt}(\mathbf{A}_t)$, and the notation introduced in Section 3.2 where we write down the price of advertising p_{jt} of channel j as a function of the amounts of advertising of different channels \mathbf{A}_t and of the total number of TV viewers $Y_t = \sum_j^J y_{jt}$: $p_{jt} \equiv$ $p_{jt} \left(\mathbf{A}_t, Y_t \left(y_{1t}(\mathbf{A}_t), ..., y_{Jt}(\mathbf{A}_t)\right)\right)$, the objective of an ASH \mathscr{H}_k at equilibrium can be written as:

$$\max_{\{A_{jt}\}_{j\in\mathscr{H}_k}}\sum_{j\in\mathscr{H}_k}\left[p_{jt}\Big(\mathbf{A}_t, Y_t\big(y_{1t}(\mathbf{A}_t), ..., y_{Jt}(\mathbf{A}_t)\big)\Big) - c_{jt}\right]A_{jt}.$$

Assuming that a pure strategy Nash equilibrium in the amount of advertising exists, and omitting the time index t for the sake of clarity, the first-order conditions (FOCs) associated with above profit maximization problem are:

$$(p_j - c_j) + \sum_{k \in \mathscr{H}_k} \left[A_k \left(\frac{\partial p_k}{\partial A_j} + \frac{\partial p_k}{\partial Y} \sum_{i, \forall i} \frac{\partial Y}{\partial y_i} \frac{\partial y_i}{\partial A_j} \right) \right] = 0, \forall j,$$
(13)

where $\frac{\partial p_k}{\partial A_j}$ measures the impact of the amount of advertising of channel j on the price of advertising seconds of channel k, $\frac{\partial p_k}{\partial Y} \frac{\partial Y}{\partial y_i}$ measures the impact of the number of viewers of channel i on the price of the advertising seconds of channel k, and $\frac{\partial y_i}{\partial A_j}$ is the impact of the amount of advertising of channel j on the number of viewers of channel i.

The above FOCs suggest that each ASH \mathscr{H}_k trades off between three effects when determining the amount of advertising A_j of channel j at equilibrium: first, the impact of A_j on the price of advertising p_j of channel j and on the price of advertising of the other channels p_k managed by the same ASH \mathscr{H}_k , through the term $\frac{\partial p_k}{\partial A_j}, \forall j \in \mathscr{H}_k$; second, the impact of A_j on the number of viewers of different TV channels y_i through the term $\frac{\partial y_i}{\partial A_j}$, $\forall i$; lastly, the impact of the number of viewers of different TV channels y_i , $\forall i$ on the price of advertising of each channel p_k of the ASH \mathscr{H}_k , through the term $\frac{\partial p_k}{\partial Y} \frac{\partial Y}{\partial y_i}$, $\forall k \in \mathscr{H}_k$.

Using the estimated preference parameters on the viewing and advertising sides $(\alpha, \sigma, \gamma_j, \gamma_{ij}, \theta_j)$, and the observed amounts and prices of advertising $(A_{jt} \text{ and } p_{jt})$, we can solve Equations (13) for the marginal costs c_{jt} .

In what follows, we make use of Equations (13) and the estimated preference parameters as well as the estimated marginal costs, to first show the impact of the two-sided network externalities between viewers and advertisers on the effects of the acquisition exhibited in Section 5.1; then, to evaluate the effectiveness of the behavioral remedy imposed by the French competition authority.

5.3 The role of two-sided network externalities

This section first presents the equilibrium level of broadcasting quality, prices and amounts of advertising following the acquisition. We then discuss how the two-sided network externalities between viewers and advertisers impact the effects of the acquisition at equilibrium. Panel 1 and Panel 2 of Table 10 summarize the different results discussed in this section.

We estimate the TV channels' broadcasting quality from our nested-logit model of viewers' demand. Formally, according to the TV viewer's utility function (Equation 1), the mean quality of channel j at time t can be measured by q_{jt} (Equation 2) and is denoted as \bar{q}_{jt} . The estimated percentage changes in \bar{q}_{jt} from 2010 to 2013 are presented in the first row of Table 10 for each of the three channels. We find a clear reallocation of quality from channel TF1 to the two purchased channels (NT1 and TMC): The quality of both channel NT1 and channel TMC has increased, while the quality of channel TF1 has decreased. Taken all together, the average quality of the three merging channels has increased by 16.5%.^{27,28}

Together with the increase in broadcasting quality of NT1 and TMC, we also observe a significant increase in their amounts and prices of advertising. (See Panel 1 of Table 10.) We could explain these rather non-standard effects of acquisition by the joint impact of the changes in broadcasting quality of the merging channels and the two-sided network externalities between viewers and advertisers.

We then simulate the consequences of the acquisition if viewers do not get disutility from advertising, to show the role of two-sided network externalities in the observed effect of the acquisition. Panel 2 of Table 10 presents the results.

The counterfactual simulation is performed according to the algorithm detailed in Appendix B.1. In the simulation, we keep the broadcasting quality of the different TV channels at the same level as in the observed equilibrium (with two-sided network externalities), so that the simulated results are directly comparable to the observed effects of the acquisition.

The equilibrium choices of the amounts of advertising by the 12 TV stations are simulated simultaneously. Our simulation procedure considers the strategic reactions between different TV

²⁷ In practice, both NT1 and TMC got the broadcasting rights to some attractive programs that might have been scheduled on channel TF1 without the acquisition. For instance, since 2011, NT1 started to broadcast some popular foreign series, such as "True Blood" and "Falling Skies", and started to offer a new culture program "Tous Différents," which is 100% produced by TF1 Group and has a significant audience; TMC got the live broadcasting rights to the marriage of Prince Albert II of Monaco with the South African swimmer Charlene Wittstock on 3 July 2011, and broadcast the movie "Bodyguard" on 13 February 2012, in tribute to the deceased singer Whitney Houston, due to the broadcast rights previously acquired by TF1 Group. Both shows generated significant peaks in audience for TMC.

 $^{^{28}}$ In this regard, the decision of the French competition authority may have boosted the competition between different TV broadcasters in terms of audience, since it may have had a positive effect on the quality of broadcasting content of the two purchased channels.

	TF1	NT1	TMC	TF1 Group average
Pan	el 1: Observ	ved equilibr	rium	
Estimated broadcasting quality (\bar{q}_{jt})	-15.03%	19.01%	10.39%	16.49%
Amount of advertising (A_{jt})	1.56%	19.37%	12.39%	10.76%
Price of advertising (p_{jt})	1.00%	59.78%	22.86%	5.68%
Panel 2: Simulated equil	ibrium in th	e absence	of two-sided	externalities
Amount of advertising (A_{jt}) Price of advertising (p_{it})	nbrium in th -10.83% 0.94%		of two-sided -2.74% 22.86%	-5.62% 5.61%
Amount of advertising (A_{jt})	-10.83% 0.94%	-3.09% 60.86%	-2.74% 22.86%	$-5.62\%\ 5.61\%$
Amount of advertising (A_{jt}) Price of advertising (p_{jt})	-10.83% 0.94%	-3.09% 60.86%	-2.74% 22.86%	$-5.62\%\ 5.61\%$

Table 10: Post-acquisition changes

Note: The percentage changes are taken over the post-acquisition years from 2010 to 2013

channels. For instance, the ASH of channel TF1 acknowledges that its amount of advertising impacts not only the number of viewers of channel TF1 but also the number of viewers of the other channels, all of which have an impact on the price of advertising of channel TF1 at equilibrium.

The simulated changes in the amounts and prices of advertising of the three merging channels from 2010 to 2013 are presented in Panel 2 of Table 10.²⁹ Comparing the simulated acquisition effects in Panel 2 to the observed acquisition effects in Panel 1, we can draw three conclusions. First, in the absence of the negative externalities that advertisers generate for viewers, the ASHs respond to the increase in advertisers' willingness to pay for the advertising slots of the merging channels (as a result of the increase in their broadcasting quality and therefore their number of viewers) by restricting the total amount of advertising slots on the merging channels and thereby increasing their prices. Second, the negative externalities that advertisers generate for viewers incentivize the ASHs to increase the amount of advertising following an increase in TV channels' broadcasting quality, as indicated by the difference between the amount of advertising (A_{jt}) in Panel 1 and Panel 2. Lastly, the joint effect of the two-sided network externalities and the changes in the broadcasting quality of the three merging channels is that both the amounts and prices of advertising of the three merging channels are increased, as presented in Panel 1.

We could explain the above findings using the FOCs derived in Section 5.2, namely, Equations (13). The broadcasting quality q_j of channel j, $\forall j$, affects the amount of advertising A_j in two ways: first, via its impact on viewers' demand elasticity with respect to A_j , and second, through its impact on the flexibility of advertising prices with respect to A_j . Specifically, the derivatives $\frac{\partial y_i}{\partial A_j}$ in Equations (13) depend on q_j according to the nested logit model for viewers'

²⁹Note that the advertising level in a given period should be higher when viewers do not care about the amount of advertising than when they do. The simulated total amount of advertising is 12.34 percent higher under the assumption that viewers do not care about the amount of advertising than in the observed equilibrium where viewers do care. The negative values in the first row of Panel 2 in Table 10 are changes in the amounts of advertising from 2010 to 2013, capturing the effects of the change in broadcasting quality of the merging channels in the absence of the negative externalities that advertisers generate for viewers.

demand in Section 3.1; the derivatives $\frac{\partial p_k}{\partial A_j}$ in Equations (13) depend on q_j , because the prices of advertising p_k , $\forall k$, are functions of the number of viewers of different TV channels according to the model for advertisers' demand in Section 3.2.

Intuitively, improving the broadcasting quality of a TV channel incentivizes its ASH to choose a higher amount of advertising, as it reduces the TV viewers' demand elasticity with respect to the amount of advertising of this channel: The value of $d\frac{\partial y_j}{\partial A_j}/dq_j$ is always negative. However, there may be an offsetting incentive for the ASH to reduce the amount of advertising but increase its price instead, due to the increase in the flexibility of the price of advertising with respect to its amount: The value of $d\frac{\partial p_j}{\partial A_j}/dq_j$ can be either positive or negative in practice. The first incentive comes from the negative externalities that the advertisers generate for the viewers. The second incentive is the direct effect of changes in the broadcasting quality of a TV channel on its amount and price of advertising (in the absence of two-sided network externalities between viewers and advertisers). Our post-acquisition data suggest that the joint effect of the two-sided network externalities and the changes in broadcasting quality of the three merging channels results in an increase in both the amounts and prices of advertising of the three merging channels at equilibrium.

5.4 Effectiveness of the behavioral remedy

This section aims to evaluate the effectiveness of the decision made by the French competition authority. In particular, we wish to comment on the effects of the behavioral remedy imposed as a counterpart to its approval of the acquisition of channels NT1 and TMC by the TF1 Group. Since our sample covers three years of the post-acquisition period (2010-2013), we observe the realized market equilibrium under the remedy requiring that the ASH of NT1 and TMC remain separate from the ASH of channel TF1. One practical way to assess the effectiveness of the implemented behavioral remedy is to compare the observed market equilibrium with a counterfactual situation in which one unique ASH determines the amounts of advertising of the three channels in order to maximize their joint profits from advertising. As we observe the quality adjustment of different TV channels following the acquisition, our counterfactual simulation (using ex-post data from 2010 to 2013) takes into account the effect of the acquisition on product quality.³⁰

The simulation is performed according to the algorithm detailed in Appendix B.2. To facilitate the comparison with the observed effects of the acquisition (given in Panel 1 of Table 10), we present directly the simulated changes from 2010 to 2013 in Panel 3 of Table $10.^{31}$

Comparing the numbers presented in Panel 3 to the numbers presented in Panel 1 allows us to reach some conclusions about the impacts of the behavioral remedy. We note that merging the ASHs of the three channels has almost no impact on their advertising prices, while their total amount of advertising increases only slightly. More precisely, merging the ASHs of the three channels increases their total amounts of advertising by 6.78% and increases their average prices by 1.41%. This result is not surprising, provided that the substitution effects of the amount of advertising on the viewers' side are small, and that the advertisers consider the advertising slots of NT1 and of TMC to be complementary to those of channel TF1. (See the demand elasticities presented in Section 4.1 and Section 4.2.) It is well known that a merger between complementary firms should not lead to a significant price increase since it eliminates a pricing externality. (See Cournot, 1838; Economides and Salop, 1992.) The slight increase in amounts of advertising after the merger of the ASHs is due to the internalization of viewers' substitution between the three

³⁰The recent literature on horizontal mergers has addressed the issue that these mergers have an impact on product quality (see Chen and Gayle, 2019).

³¹We have carefully checked that the simulated amounts of advertising are below the maximum levels imposed by the regulator.

channels.

The behavioral remedy was adopted to prevent anti-competitive effects that a common ASH for the three merging channels could potentially cause in the TV advertising market. The competition authority worried that merging the ASHs of the three channels might disadvantage the other competing ASHs and the consumers (viewers and advertisers). We now evaluate the welfare effects of the acquisition and the behavioral remedy in order to draw some conclusions about the effectiveness of the merger decision. We can evaluate the variation in viewer surplus from our nested-logit model, as in Small and Rosen (1981): $CS__{viewers} = -\frac{1}{\alpha}ln[1 + \sum_{g}[\sum_{j \in g} \exp(\frac{q_{jt} + \alpha A_{jt}}{(1 - \sigma)})]^{(1 - \sigma)}]$. The variation in advertisers' surplus can be estimated by $C_t = \sum_{j} p_{jt} \times A_{jt}$, which measures their total advertising cost. The profit of an ASH \mathscr{H}_k is given by Equation (12): $\Pi_{kt} = \sum_{j \in \mathscr{H}_k} (p_{jt} - c_{jt}) A_{jt}$. The estimated welfare changes following the acquisition (from 2010 to 2013) under the be-

The estimated welfare changes following the acquisition (from 2010 to 2013) under the behavioral remedy (merging only the broadcasting services of the three channels) and without the behavioral remedy (merging both the broadcasting services and the ASHs of the three channels) are presented in Table 11.

Table 11: Welfare changes from 2010 to 2013

	Viewers' surplus	Total cost of advertisements	Total profit (TF1 Group)	Total profit (others)
Observed merger under remedy	-7.94%	13.26%	4.03%	71.18%
Simulated merger without remedy	-8.33%	-0.08%	10.13%	-3.22%

Note: Results in the first row are computed from the observed equilibrium, results in the second row are computed from the simulated equilibrium, presented in Panel 3 of Table 10.

The first row of Table 11 presents the welfare effects of the acquisition under the behavioral remedy, i.e., the welfare effects of merging only the broadcasting services of channels NT1, TMC and TF1. The changes in viewers' surplus in the first row indicate that the surplus of TV viewers has decreased following the acquisition. This is, firstly, because the TF1 Group reallocated some high-quality programs from channel TF1 to the two purchased channels, so the broadcasting quality of its major channel (which is also the most popular channel of the market) decreased following the acquisition. In addition, the total amount of advertising increased from 2010 to 2013, which negatively impacted the surplus of TV viewers as well. The presented change in the total cost of advertisements suggests that the advertisers' total costs increased from 2010 to 2013. This is because both the market average amount and price of advertising have increased following the acquisition.

The second row of Table 11 presents the welfare effects of the acquisition without the behavioral remedy, i.e., the welfare effects of merging both the broadcasting services and the ASHs of channels NT1, TMC and TF1. Considering the difference between the results in the second row and the results in the first row, we can conclude that the remedy did not have a significant positive effect on the surplus of TV viewers, but significantly increased the total cost for the advertisers. If there were one common ASH which maximized the joint profits from the advertisement slots of the three channels, the other non-merging ASHs would have to reduce their amounts of advertising and prices to attract viewers and advertisers following the acquisition, as strategic reactions to the amount of advertising profits of the ASH of TF1 Group would be higher, while those of the other non-merging ASHs would be lower than in the case in which two separate ASHs manage the advertising slots of channels NT1, TMC and TF1 (i.e., the results in the first row of Table 11). Our finding suggests that the implemented behavioral remedy has benefited the ASHs of TF1 Group's competitors, but

has disadvantaged advertisers.

6 Conclusion

This paper contributes to the analysis of mergers in two-sided markets by assessing a decision of the French competition authority, which approved the merger of the broadcasting services of three TV channels but has de facto prohibited the merger of their ASHs via a behavioral remedy.

To do so, we first build a structural model which accounts for the multi-homing behavior of advertisers. We then estimate the demands of viewers and advertisers using a comprehensive data set. This step allows us to confirm that one should consider TV channels as two-sided market platforms since we show that advertising has significant negative externalities on TV viewers. Using ex-post data, we evaluate the consequences of the acquisition. We show that the acquisition had a positive effect on the average broadcasting quality of merging channels; however, blocking the merger of their ASHs through a behavioral remedy has been ineffective at limiting the increase in their prices and amounts of advertising.

Based on a counterfactual simulation of the market equilibrium in the absence of the negative externalities that advertisers generate for viewers, we show how the ASHs respond to the increase in advertisers' willingness to pay (as a result of the increase in the merging channels' broadcasting quality and therefore their viewership) by restricting the total amount of advertising slots on the merging channels and thereby increasing their prices. We further show that the two-sided network externalities between viewers and advertisers incentivize the ASHs to increase the amounts of advertising of the merging channels as well (as a result of the increase in their broadcasting quality) since viewers are less sensitive to the amounts of advertising during programs of better quality. Regardless of the behavioral remedy aiming at limiting any detrimental effect of the acquisition on the advertising side of the market, the joint effect of the increase in the broadcasting quality of the merging channels and the two-sided network externalities between viewers and advertisers results in an increase in both the amounts and prices of advertising of the merging channels.

To comment on the effectiveness of the behavioral remedy, we counterfactually simulate the acquisition under the assumption that the merger on the advertising side was also approved. Our results suggest that the remedy enforced by the French competition authority did not have a significant positive effect on the surplus of TV viewers but increased advertisers' total cost. We note, however, that merging the ASHs of the three TV channels involved in the acquisition would have shifted advertising profits of the non-merging ASHs to the merging ones. On the basis of European competition law, the French competition authority should have approved the merger of the ASHs of the three channels, since the consumer surplus remained almost unchanged. However, in the political debate, a decision about whether to approve this merger could be determined according to the weights that the people allocate to the different market players. In any case, the two-sided nature of the market should not be ignored when examining the merger.

Hence, the main lesson of our analysis is that, in the process of designing competition or regulatory policy for two-sided markets, ignoring the interaction between the two sides of platforms can result in unexpected outcomes.

This conclusion is drawn from the study of the digital TV industry. Provided more disaggregated data on audience and advertising were available, further investigation to refine this analysis could be undertaken. We expect our methodology could also be helpful for examining similar markets, especially those in which the usage of services on one side is free and all the revenues come from the other side.

Appendix A: Additional tables and figures

		2008	2009	2010	2011	2012	2013
Incumbents	Channel 1	50.9%	43.5%	53.6%	53.8%	43.3%	44.4%
	Channel 2	41.0%	29.9%	38.1%	38.6%	35.6%	39.1%
	Channel 3	20.0%	22.1%	28.2%	29.7%	27.6%	27.7%
	Channel 4	83.7%	56.9%	64.7%	58.3%	56.4%	70.1%
	Channel 5	92.6%	67.7%	73.6%	69.7%	71.6%	75.3%
\mathbf{New}	Channel 6	23.5%	33.6%	39.6%	43.5%	59.0%	74.7%
entrants	Channel 7	34.3%	35.3%	33.2%	30.5%	33.2%	43.4%
	Channel 8	33.0%	34.0%	37.8%	49.2%	62.5%	54.9%
	Channel 9	19.8%	29.8%	38.0%	35.3%	29.2%	37.6%
	Channel 10	18.3%	19.6%	20.2%	24.5%	31.6%	38.4%
	Channel 11	36.6%	45.2%	48.7%	52.0%	70.0%	77.5%
	Channel 12	41.9%	44.3%	52.0%	50.1%	69.0%	77.9%

Table A1: Ratio of observed amounts of advertising to authorized ceilings

Note: The names of TV channels are not reported for confidentiality reasons.

Table A2: Audience shares of incumbent channels and new-entrant channels

Year	Channel	Audier	ice shares
		Mean	Std. Dev.
2008	Incumbent	13.2%	0.074
	New	1.2%	0.005
2009	Incumbent	12.7%	0.071
	New	1.5%	0.006
2010	Incumbent	12.1%	0.067
	New	1.7%	0.007
2011	Incumbent	11.6%	0.063
	New	2.2%	0.007
2012	Incumbent	11.5%	0.060
	New	2.2%	0.007
2013	Incumbent	11.2%	0.060
	New	2.2%	0.008

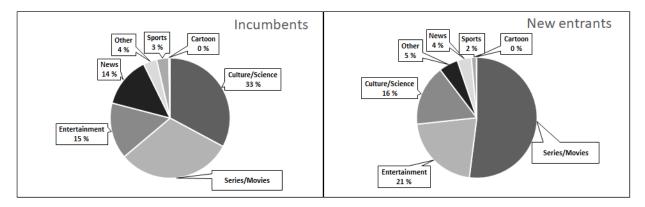


Figure A.1: Distribution of program genres of incumbents and new entrants

	A_{jt}	$\ln \bar{s}_{jt/g}$
Entertainment of all competing channels	-0.529***	0.034^{***}
	(0.056)	(0.012)
News of all competing channels	0.596^{***}	-0.029
	(0.107)	(0.024)
Entertainment of competing channels	-0.252***	0.046**
in a group	(0.032)	(0.023)
News of competing channels in a group	0.197^{***}	-0.022*
	(0.049)	(0.012)
Broadcasting hours of different programs	Yes	Yes
Channel FE	Yes	Yes
Month FE	Yes	Yes
Year FE	Yes	Yes
No. observations	840	840

Table A2.	Finat atom	actimation	-af TV	miomona?	damand
Table As.	FITSU STAR	e estimation		viewers	uemanu

Note: Standard errors of estimates are in parentheses: ***p < 0.01, **p < 0.05, *p < 0.1

	(OLS)	(IV)
	$\ln s_{jt} - \ln s_{0t}$	$\ln s_{jt} - \ln s_{0t}$
Amount of advertising (α)	0.052***	-0.111***
	(0.008)	(0.031)
Within-nest share (σ)	1.025***	0.636***
	(0.038)	(0.192)
Broadcasting hours of different programs	Yes	Yes
Channel FE	Yes	Yes
Month FE	Yes	Yes
Year FE	Yes	Yes
No. observations	840	840

Table A4: OLS versus IV estimation of TV viewers' demand

Note: Standard errors of estimates are in parentheses: ***p < 0.01, **p < 0.05, *p < 0.1

	Baseline estimation	Robustness check
	(same IVs as in Table 5)	(Additional IVs)
Amount of advertising (α)	-0.111***	-0.121***
	(0.031)	(0.031)
Within-nest share (σ)	0.636***	0.659***
	(0.192)	(0.193)
${ m TV}~{ m Series}/{ m Movies}$	0.003	0.003
	(0.003)	(0.003)
$\operatorname{Culture}/\operatorname{Science}$	0.001	0.002
	(0.004)	(0.004)
News	0.068***	0.070***
	(0.009)	(0.009)
Entertainment	-0.255***	-0.260***
	(0.078)	(0.079)
Sports	0.011	0.012
-	(0.009)	(0.009)
Cartoons	0.461^{**}	0.473***
	(0.111)	(0.113)
Channel FE	Yes	Yes
Month FE	Yes	Yes
Year FE	Yes	Yes
No. observations	840	840
Cragg–Donald Wald F statistic	14.665	11.914
Hansen J statistic (p -value)	0.440	0.303

Table A5: Robustness check for the viewers' demand estimation

Note: The second column presents the estimates using monthly broadcasting hours of news and entertainment of all competing channels, as well as monthly broadcasting hours of news and entertainment of all competing channels in a group (incumbent or entrant). The third column presents the estimates using one additional set of IVs: monthly broadcasting hours of TV series/movies of all competing channels; monthly broadcasting hours of TV series/movies of all competing channels in a group (incumbent or entrant). Including more IVs than were used in Table 6 results in similar estimates but decreases the Cragg–Donald Wald F statistics. Standard errors of estimates are in parentheses: ***p < 0.01, **p < 0.05, *p < 0.1

	$\ln p_{TF1}^t$	$\ln p_{FR2}^t$	$\ln p_{FR3}^t$	$\ln p_{M6}^t$	$\ln p_{FR5}^t$	$\ln p_{D8}^t$	$\ln p_{NT1}^t$	$\ln p_{FR4}^t$	$\ln p_{TMC}^t$	$\ln p^t_{Gulli}$	$\ln p_{D17}^t$	$\ln p_{W9}^t$
$\ln p_{TF1}^{t-2}$	0.248 (0.10)	$0.181 \\ (0.47)$	$0.501 \\ (0.55)$	$0.265 \\ (0.44)$	$0.481 \\ (0.61)$	$\begin{array}{c} 0.328 \\ (0.38) \end{array}$	$0.075 \\ (0.27)$	-1.245 (0.60)	-0.176 (0.28)	$0.329 \\ (0.44)$	$\begin{array}{c} 0.333 \ (0.31) \end{array}$	-0.134 (0.45)
$\ln p_{FR2}^{t-2}$	-0.869 (0.04)	-0.935 (0.41)	-1.183 (0.49)	-0.980 (0.39)	-1.525 (0.54)	-0.914 (0.34)	-0.565 (0.24)	-0.379 (0.53)	-0.553 (0.25)	-0.236 (0.38)	-0.481 (0.27)	-0.968 (0.40)
$\ln p_{FR3}^{t-2}$	$\begin{array}{c} 0.513 \ (0.40) \end{array}$	-0.105 (0.41)	$\begin{array}{c} 0.434 \\ (0.28) \end{array}$	$\begin{array}{c} 0.252 \\ (0.39) \end{array}$	$\begin{array}{c} 0.351 \ (0.53) \end{array}$	$\begin{array}{c} 0.395 \ (0.33) \end{array}$	$\begin{array}{c} 0.221 \\ (0.23) \end{array}$	$\begin{array}{c} 0.321 \ (0.53) \end{array}$	$\begin{array}{c} 0.220 \\ (0.25) \end{array}$	$\begin{array}{c} 0.198 \\ (0.38) \end{array}$	$\begin{array}{c} 0.185 \ (0.27) \end{array}$	$\begin{array}{c} 0.194 \\ (0.39) \end{array}$
$\ln p_{M6}^{t-2}$	-0.09 (0.44)	$0.445 \\ (0.45)$	$\begin{array}{c} 0.068 \ (0.54) \end{array}$	$\begin{array}{c} 0.351 \\ (0.23) \end{array}$	-0.121 (0.59)	-0.019 (0.37)	$\begin{array}{c} 0.012 \\ (0.26) \end{array}$	$\begin{array}{c} 0.775 \ (0.58) \end{array}$	$\begin{array}{c} 0.312 \ (0.27) \end{array}$	$0.569 \\ (0.42)$	-0.005 (0.30)	$0.925 \\ (0.44)$
$\ln p_{FR5}^{t-2}$	-0.178 (0.29)	$\begin{array}{c} 0.014 \ (0.30) \end{array}$	-0.210 (0.35)	-0.106 (0.28)	$\begin{array}{c} 0.230 \\ (0.18) \end{array}$	-0.097 (0.24)	-0.150 (0.17)	$\begin{array}{c} 0.058 \\ (0.38) \end{array}$	-0.234 (0.18)	-0.890 (0.28)	-0.338 (0.20)	-0.324 (0.29)
$\frac{\ln p_{D8}^{t-2}}{7}$	-0.285 (0.18)	-0.652 (0.19)	-0.433 (0.22)	-0.289 (0.18)	-0.738 (0.24)	$0.569 \\ (0.15)$	-0.106 (0.11)	-0.197 (0.24)	$\begin{array}{c} 0.007 \\ (0.11) \end{array}$	-0.032 (0.17)	-0.107 (0.12)	-0.300 (0.18)
$\ln p_{NT1}^{t-2}$	$\begin{array}{c} 0.422 \\ (0.37) \end{array}$	$\begin{array}{c} 0.158 \\ (0.38) \end{array}$	$\begin{array}{c} 0.085 \\ (0.45) \end{array}$	$\begin{array}{c} 0.334 \\ (0.36) \end{array}$	$\begin{array}{c} 0.481 \\ (0.49) \end{array}$	$\begin{array}{c} 0.339 \ (0.31) \end{array}$	$\begin{array}{c} 0.943 \\ (0.022) \end{array}$	$0.646 \\ (0.48)$	$\begin{array}{c} 0.196 \\ (0.23) \end{array}$	$\begin{array}{c} 0.501 \\ (0.35) \end{array}$	$1.250 \\ (0.25)$	$\begin{array}{c} 0.231 \\ (0.36) \end{array}$
$\ln p_{FR4}^{t-2}$	-0.078 (0.10)	-0.140 (0.10)	$\begin{array}{c} 0.016 \\ (0.12) \end{array}$	-0.012 (0.10)	-0.114 (0.13)	-0.133 (0.08)	-0.051 (0.06)	$\begin{array}{c} 0.691 \\ (0.13) \end{array}$	-0.009 (0.06)	-0.131 (0.10)	-0.064 (0.07)	-0.170 (0.10)
$\ln p_{TMC}^{t-2}$	-0.367 (0.43)	-0.340 (0.44)	-0.575 (0.52)	-0.287 (0.42)	-0.523 (0.57)	-0.132 (0.36)	-0.061 (0.25)	-0.888 (0.56)	$\begin{array}{c} 0.366 \\ (0.21) \end{array}$	-0.829 (0.41)	-0.723 (0.29)	-0.428 (0.42)
$\ln p_{Gulli}^{t-2}$	$\begin{array}{c} 0.217 \\ (0.17) \end{array}$	$0.239 \\ (0.17)$	$0.297 \\ (0.20)$	$0.296 \\ (0.16)$	$\begin{array}{c} 0.128 \\ (0.22) \end{array}$	-0.171 (0.14)	$\begin{array}{c} 0.107 \\ (0.10) \end{array}$	$\begin{array}{c} 0.453 \\ (0.22) \end{array}$	$0.228 \\ (0.10)$	$0.384 \\ (0.16)$	-0.034 (0.11)	$0.264 \\ (0.17)$
$\ln p_{D17}^{t-2}$	$\begin{array}{c} 0.215 \\ (0.22) \end{array}$	$\begin{array}{c} 0.351 \ (0.23) \end{array}$	$\begin{array}{c} 0.273 \ (0.27) \end{array}$	$\begin{array}{c} 0.170 \\ (0.22) \end{array}$	$0.449 \\ (0.29)$	$0.290 \\ (0.18)$	$0.184 \\ (0.13)$	-0.037 (0.29)	$\begin{array}{c} 0.121 \\ (0.14) \end{array}$	-0.034 (0.21)	$0.280 \\ (0.15)$	$\begin{array}{c} 0.350 \\ (0.22) \end{array}$
$\ln p_{W9}^{t-2}$	-0.008 (0.26)	$0.265 \\ (0.26)$	$0.158 \\ (0.31)$	$0.059 \\ (0.25)$	$\begin{array}{c} 0.348 \\ (0.34) \end{array}$	0.044 (0.21)	-0.173 (0.15)	-0.101 (0.34)	-0.072 (0.16)	$\begin{array}{c} 0.105 \\ (0.24) \end{array}$	0.024 (0.17)	$0.304 \\ (0.15)$
$\ln Y$	Yes	Yes quation:	Yes 67	Yes	Yes	Yes						

Table A6: First stage estimation of advertisers' demand with twice lagged prices as IVs

Note: Standard errors of estimates are in parentheses.

	$\ln p_{TF1}^t$	$\ln p_{FR2}^t$	$\ln p_{FR3}^t$	$\ln p_{M6}^t$	$\ln p_{FR5}^t$	$\ln p_{D8}^t$	$\ln p_{NT1}^t$	$\ln p_{FR4}^t$	$\ln p_{TMO}^t$	$c \ln p^t_{Gulli}$	$\ln p_{D17}^t$	$\ln p_W^t$
News_TF1	0.148 (0.04)	$\begin{array}{c} 0.186 \\ (0.05) \end{array}$	$\begin{array}{c} 0.113 \\ (0.07) \end{array}$	$0.066 \\ (0.04)$	$\begin{array}{c} 0.167 \\ (0.05) \end{array}$	-0.041 (0.06)	$\begin{array}{c} 0.037 \\ (0.05) \end{array}$	-0.040 (0.11)	$\begin{array}{c} 0.024 \\ (0.05) \end{array}$	-0.021 (0.07)	$0.098 \\ (0.06)$	0.158 (0.06)
News_FR2	$\left \begin{array}{c} 0.011 \\ (0.03) \end{array} \right $	-0.043 (0.04)	-0.013 (0.06)	-0.037 (0.03)	-0.035 (0.04)	$\begin{array}{c} 0.117 \\ (0.05) \end{array}$	-0.028 (0.04)	-0.050 (0.09)	$\begin{array}{c} 0.009 \\ (0.04) \end{array}$	$0.051 \\ (0.06)$	-0.003 (0.05)	-0.025 (0.05)
News_FR3	$\left \begin{array}{c} 0.045 \\ (0.04) \end{array} \right $	$\begin{array}{c} 0.024 \\ (0.05) \end{array}$	-0.057 (0.06)	$\begin{array}{c} 0.008 \\ (0.04) \end{array}$	$\begin{array}{c} 0.020 \\ (0.05) \end{array}$	$\begin{array}{c} 0.188 \\ (0.05) \end{array}$	$\begin{array}{c} 0.094 \\ (0.04) \end{array}$	-0.037 (0.10)	$\begin{array}{c} 0.101 \\ (0.04) \end{array}$	-0.014 (0.06)	$\begin{array}{c} 0.078 \\ (0.05) \end{array}$	0.089 (0.06
News_M6	$ \begin{array}{c c} 0.139 \\ (0.04) \end{array} $	$\begin{array}{c} 0.206 \\ (0.04) \end{array}$	$\begin{array}{c} 0.112 \\ (0.06) \end{array}$	$\begin{array}{c} 0.090 \\ (0.03) \end{array}$	$\begin{array}{c} 0.190 \\ (0.05) \end{array}$	$\begin{array}{c} 0.039 \\ (0.05) \end{array}$	$\begin{array}{c} 0.083 \\ (0.04) \end{array}$	-0.044 (0.10)	$\begin{array}{c} 0.068 \\ (0.04) \end{array}$	$0.082 \\ (0.06)$	$\begin{array}{c} 0.100 \\ (0.05) \end{array}$	$0.150 \\ (0.06$
News_FR5	-0.022 (0.23)	-0.168 (0.27)	$\begin{array}{c} 0.274 \\ (0.39) \end{array}$	$0.068 \\ (0.21)$	$\begin{array}{c} 0.098 \\ (0.31) \end{array}$	$\begin{array}{c} 0.042 \\ (0.32) \end{array}$	-0.239 (0.26)	$0.669 \\ (0.61)$	$0.178 \\ (0.25)$	$\begin{array}{c} 0.410 \\ (0.38) \end{array}$	-0.604 (0.32)	-0.21 (0.36
News_D8	0.047 (0.02)	$\begin{array}{c} 0.040 \\ (0.03) \end{array}$	$\begin{array}{c} 0.011 \\ (0.04) \end{array}$	$0.006 \\ (0.02)$	$\begin{array}{c} 0.077 \\ (0.03) \end{array}$	$\begin{array}{c} 0.057 \\ (0.02) \end{array}$	$\begin{array}{c} 0.017 \\ (0.03) \end{array}$	-0.055 (0.06)	$\begin{array}{c} 0.011 \\ (0.03) \end{array}$	-0.033 (0.04)	$\begin{array}{c} 0.020 \\ (0.03) \end{array}$	0.028 (0.04
News_NT1	0.077 (0.03)	$\begin{array}{c} 0.060 \\ (0.04) \end{array}$	$\begin{array}{c} 0.029 \\ (0.06) \end{array}$	$\begin{array}{c} 0.030 \\ (0.03) \end{array}$	$\begin{array}{c} 0.055 \\ (0.04) \end{array}$	$\begin{array}{c} 0.180 \\ (0.05) \end{array}$	$0.058 \\ (0.03)$	$\begin{array}{c} 0.016 \\ (0.09) \end{array}$	$\begin{array}{c} 0.076 \ (0.04) \end{array}$	-0.015 (0.06)	$\begin{array}{c} 0.077 \\ (0.05) \end{array}$	0.090 (0.05
News_FR4	0.142 (0.13)	$\begin{array}{c} 0.127 \\ (0.15) \end{array}$	$\begin{array}{c} 0.299 \\ (0.22) \end{array}$	$\begin{array}{c} 0.280 \\ (0.12) \end{array}$	$\begin{array}{c} 0.010 \\ (0.17) \end{array}$	-0.282 (0.18)	$\begin{array}{c} 0.149 \\ (0.14) \end{array}$	$\begin{array}{c} 0.576 \ (0.34) \end{array}$	$\begin{array}{c} 0.130 \\ (0.14) \end{array}$	0.059 (0.22)	-0.083 (0.18)	0.180 (0.20)
News_TMC	0.079 (0.03)	$\begin{array}{c} 0.117 \\ (0.03) \end{array}$	$\begin{array}{c} 0.058 \\ (0.05) \end{array}$	$\begin{array}{c} 0.035 \ (0.03) \end{array}$	$\begin{array}{c} 0.125 \\ (0.04) \end{array}$	$\begin{array}{c} 0.053 \\ (0.04) \end{array}$	$\begin{array}{c} 0.039 \\ (0.03) \end{array}$	-0.045 (0.08)	$\begin{array}{c} 0.015 \\ (0.03) \end{array}$	$0.022 \\ (0.05)$	$\begin{array}{c} 0.114 \\ (0.04) \end{array}$	$0.060 \\ (0.04)$
News_Gulli	-0.447 (0.16)	-0.462 (0.19)	-0.528 (0.27)	-0.370 (0.15)	-0.590 (0.21)	$0.002 \\ (0.22)$	-0.017 (0.18)	-0.875 (0.42)	-0.253 (0.18)	$\begin{array}{c} 0.250 \\ (0.17) \end{array}$	$\begin{array}{c} 0.258 \\ (0.23) \end{array}$	-0.22 (0.25
News_D17	-0.265 (0.13)	-0.142 (0.04)	-0.345 (0.22)	-0.199 (0.12)	-0.241 (0.18)	-0.216 (0.19)	-0.219 (0.15)	-0.281 (0.35)	-0.311 (0.15)	-0.614 (0.22)	-0.470 (0.19)	-0.27 (0.11
News_W9	0.122 (0.04)	$\begin{array}{c} 0.142 \\ (0.04) \end{array}$	$0.078 \\ (0.06)$	$\begin{array}{c} 0.051 \\ (0.03) \end{array}$	0.214 (0.05)	-0.060 (0.05)	0.079 (0.04)	$\begin{array}{c} 0.127 \\ (0.09) \end{array}$	-0.003 (0.04)	-0.053 (0.06)	$\begin{array}{c} 0.073 \\ (0.05) \end{array}$	$0.161 \\ (0.06$
Ent_TF1	0.018 (0.02)	$\begin{array}{c} 0.041 \\ (0.02) \end{array}$	$\begin{array}{c} 0.026 \\ (0.04) \end{array}$	$0.008 \\ (0.02)$	$\begin{array}{c} 0.041 \\ (0.03) \end{array}$	-0.075 (0.03)	-0.010 (0.02)	-0.057 (0.05)	-0.022 (0.02)	-0.034 (0.03)	-0.030 (0.03)	-0.03 $(0.03$
$\operatorname{Ent}_{\operatorname{FR2}}$	-0.015 (0.02)	$\begin{array}{c} 0.041 \\ (0.03) \end{array}$	-0.013 (0.04)	-0.031 (0.022)	$\begin{array}{c} 0.028 \\ (0.03) \end{array}$	-0.131 (0.03)	-0.037 (0.03)	-0.074 (0.06)	-0.090 (0.03)	-0.106 (0.04)	-0.022 (0.03)	-0.08 (0.04
${ m Ent}_{ m FR3}$	0.021 (0.03)	$\begin{array}{c} 0.013 \\ (0.04) \end{array}$	$0.045 \\ (0.06)$	$0.009 \\ (0.03)$	$\begin{array}{c} 0.022 \\ (0.04) \end{array}$	-0.074 (0.05)	-0.051 (0.04)	$\begin{array}{c} 0.088 \\ (0.09) \end{array}$	-0.004 (0.04)	-0.069 (0.06)	-0.066 (0.05)	-0.04 (0.05
Ent_M6	0.028 (0.03)	$0.059 \\ (0.03)$	$0.050 \\ (0.05)$	-0.002 (0.03)	$0.036 \\ (0.04)$	-0.138 (0.04)	-0.029 (0.03)	-0.097 (0.08)	-0.047 (0.03)	-0.025 (0.05)	-0.008 (0.04)	-0.02 (0.05
Ent_FR5	-0.122 (0.18)	-0.340 (0.22)	-0.230 (0.32)	0.041 (0.18)	-0.295 (0.03)	$0.849 \\ (0.26)$	$0.214 \\ (0.21)$	$\begin{array}{c} 0.723 \\ (0.50) \end{array}$	$0.421 \\ (0.21)$	$0.404 \\ (0.31)$	$\begin{array}{c} 0.213 \\ (0.26) \end{array}$	0.478 (0.30
Ent_D8	-0.037 (0.02)	-0.001 (0.029)	-0.038 (0.04)	-0.031 (0.02)	-0.005 (0.03)	-0.047 (0.03)	-0.009 (0.03)	-0.105 (0.06)	-0.065 (0.03)	-0.027 (0.04)	-0.003 (0.03)	-0.04 (0.04
Ent_NT1	0.042 (0.03)	$\begin{array}{c} 0.031 \\ (0.04) \end{array}$	0.050 (0.05)	$\begin{array}{c} 0.022 \\ (0.03) \end{array}$	$0.056 \\ (0.04)$	-0.111 (0.04)	-0.027 (0.03)	-0.020 (0.08)	-0.059 (0.03)	-0.062 (0.05)	-0.062 (0.04)	-0.10 (0.05
Ent_FR4	0.024 (0.02)	$\begin{array}{c} 0.022 \\ (0.03) \end{array}$	0.009 (0.04)	0.004 (0.02)	0.023 (0.03)	-0.017 (0.03)	-0.024 (0.03)	-0.116 (0.06)	-0.050 (0.03)	-0.093 (0.04)	$0.008 \\ (0.03)$	-0.03 (0.04
Ent_TMC	0.020 (0.04)	0.084 (0.04)	0.054 (0.06)	-0.007 (0.04)	0.060 (0.05)	-0.189 (0.05)	-0.028 (0.04)	0.150 (0.10)	-0.059 (0.03)	-0.054 (0.06)	-0.059 (0.05)	-0.02 (0.06
Ent_Gulli	-0.012 (0.03)	0.014 (0.04)	0.017 (0.054)	-0.037 (0.03)	0.000 (0.04)	-0.042 (0.04)	-0.026 (0.04)	-0.090 (0.08)	-0.013 (0.04)	-0.062 (0.05)	-0.011 (0.04)	-0.06 (0.05
Ent_D17	0.032 (0.02)	0.026 (0.02)	0.017 (0.05)	0.021 (0.02)	0.024 (0.03)	-0.019 (0.03)	-0.015 (0.03)	-0.121 (0.05)	-0.023 (0.02)	0.018 (0.03)	-0.006 (0.03)	-0.02
Ent_W9	(0.02) 0.016 (0.02)	0.038 (0.03)	0.049 (0.03)	0.003	(0.027 (0.03)	-0.067 (0.03)	(0.024) (0.03)	-0.063 (0.06)	-0.025 (0.03)	-0.038 (0.04)	(0.037 (0.03)	-0.03
$\ln Y$	Yes Yes	(0.09) Yes	Yes	(0.02) Yes <u>Nu</u>	(0.05) Yes	Yes	Yes	Yes	(0.05) Yes	Yes	Yes	Yes

Table A7: First stage estimation of advertisers' demand with competitors' broadcasting content as IVs

	Advert Qua	antity	Advert Price	e
	(percent ch	ange)	(percent cha	ange)
	coeff.	(s.e.)	coeff.	(s.e.)
$TF1 \times Acquisition$	27.05***	(0.096)	23.83***	(0.096)
$NT1 \times Acquisition$	52.60***	(0.116)	134.44***	(0.182)
$TMC \times Acquisition$	43.74***	(0.109)	115.84***	(0.168)
Others imes Acquisition	Yes		Yes	
Channel FE	Yes		Yes	
Month -Year FE	Yes		Yes	

Table A8: Effects of the acquisition on the amounts and prices of advertising (01.2011-12.2013)

Note: The percentage amount of advertising and price effects are obtained from a transformation of the parameters ρ_j and λ_j using $\exp(\rho_j) - 1$ and $\exp(\lambda_j) - 1$. Standard errors are computed using the delta method. ***p < 0.01, **p < 0.05, *p < 0.1

Appendix B.1: Simulating the acquisition under inelastic viewers' demand

The simulation can be performed using the FOCs derived in Section 5.1, namely, Equation (13). Assuming that the viewers' demand is inelastic to advertising implies that the term $\frac{\partial y_i}{\partial A_j}$ is equal to 0, $\forall i$. Omitting the time index t for the sake of clarity, Equation (13) can be simplified as:

$$(p_j - c_j) + \sum_{k \in \mathscr{H}_k} A_k \frac{\partial p_k}{\partial A_j} = 0, \forall j.$$
(14)

In more detail, we first set the disutility of advertising to TV viewers, α , to 0 and compute the resulting viewership of the different TV channels $y_{jt}(\bar{q}_{jt})$ according to the nested logit model: $y_{jt} = \frac{T_t \exp(\delta_{jt}/(1-\sigma))}{D_{gt}^{\sigma}[\sum_g D_{gt}^{(1-\sigma)}]}$, where T_t denotes the total population, $D_{gt} = \sum_{j \in g} \exp[\delta_{jt}/(1-\sigma)]$, and $\delta_{jt} = \bar{q}_{jt}$ (\bar{q}_{jt} is estimated as in Section 5.3.) Next, we hold fixed the value of $y_{jt}(\bar{q}_{jt})$, the estimated preference parameters (σ , γ_j , γ_{ij} , θ_j), and marginal costs (c_{jt}), but vary A_{jt} and p_{jt} until we find their optimal levels at the counterfactual equilibrium. In practice, we can write down the advertising price p_{jt} of channel j at time t as a function of $\mathbf{A}_t = (A_{1t}, ..., A_{Jt})$: $p_{jt} = f(\mathbf{A}_t, \bar{Y}_t)$, where $\bar{Y}_t = \sum_j^J y_{jt}(\bar{q}_{jt})$, according to the advertisers' cost share equations defined by Equation (8). In other words, Equations (14) can be written as:

$$\mathscr{F}(\mathbf{A}_t, p_{jt}(\mathbf{A}_t, \bar{Y}_t)) = 0, \forall j.$$
(15)

We numerically search for \mathbf{A}_t^* which solves Equation (15). The detailed simulation procedure is as follows:

- 1. Choose a vector of starting values of \mathbf{A}_t (we use the observed \mathbf{A}_t);
- 2. Search for $\mathbf{p_t}$ which satisfies the advertisers' demand: $\frac{p_{jt}A_{jt}}{\sum_i p_{jt}A_{jt}} = \gamma_j + \sum_i^J \gamma_{ij} \ln p_{it} + \theta_j (\ln \bar{Y}_t);$

3. Compute $\mathscr{F}(\mathbf{A}_t, p_{jt}(\mathbf{A}_t, \bar{Y}_t));$

4. Iterate until $\mathscr{F}(\mathbf{A}_t, p_{jt}(\mathbf{A}_t, \bar{Y}_t)) = 0.$

The simulated changes in amounts and prices of advertising of the three merging channels from 2010 to 2013 are presented in Panel 2 of Table 10 above.³²

 $^{^{32}}$ We have carefully checked that the simulated amounts of advertising are below the maximum levels imposed by the regulator.

Appendix B.2: Simulating the merger without the behavioral remedy

The merger simulation is performed using the FOCs described in Section 5.2, namely, Equation (13). We assume that there is one common ASH for TF1 Group, which maximizes the joint profits of channels NT1, TMC and TF1. We hold fixed the estimated preference parameters (α , σ , γ_{jj}) and marginal costs (c_{jt}), but vary the numbers of TV viewers y_{jt} , amounts of advertising A_{jt} , and prices p_{jt} , until we find their optimal levels at the counterfactual equilibrium. In practice, we can write down y_{jt} and p_{jt} of channel j at time t as functions of the $\mathbf{A}_t = (A_{1t}, ..., A_{Jt})$: $y_{jt} = f_1(\mathbf{A}_t, \bar{q}_{jt})$ according to the nested logit model for viewers' demand defined in Equation (5) and $p_{jt} = f_2(\mathbf{A}_t, Y_t(\mathbf{A}_t))$ according to the advertisers' cost share equations given by Equation (8). In other words, Equations (13) can be written as:

$$\mathscr{F}(\mathbf{A}_t, p_{jt}(\mathbf{A}_t, Y_t(\mathbf{A}_t))) = 0, \forall j.$$
(16)

We numerically search for \mathbf{A}_t^* which solves the Equation (16). The detailed simulation procedure is as follows:

- 1. Guess a vector of starting values of \mathbf{A}_t (we use the observed \mathbf{A}_t in data);
- 2. Compute $y_{jt}(\mathbf{A}_t, \bar{q}_{jt}), \forall jt$ according to the nested logit model: $y_{jt} = \frac{T_t \exp(\delta_{jt}/(1-\sigma))}{D_{gt}^{\sigma}[\sum_g D_{gt}^{(1-\sigma)}]}$, where T_t denotes the total population, $D_{gt} = \sum_{j \in g} \exp[\delta_{jt}/(1-\sigma)], \delta_{jt} = \bar{q}_{jt} + \alpha A_{jt};$ $(\bar{q}_{jt} \text{ is estimated as in Section 5.1; we hold its value fixed in the simulation})$
- 3. Compute $Y_t = \sum_j^J y_{jt}(\mathbf{A}_t, \bar{q}_{jt});$
- 4. Search for $\mathbf{p_t}$ which satisfies the advertisers' demand: $\frac{p_{jt}A_{jt}}{\sum_{i}p_{jt}A_{jt}} = \gamma_j + \sum_{i}^{J} \gamma_{ij} \ln p_{it} + \theta_j (\ln Y_t);$
- 5. Compute $\mathscr{F}(\mathbf{A}_t, p_{jt}(\mathbf{A}_t, Y_t(\mathbf{A}_t)));$
- 6. Iterate until $\mathscr{F}(\mathbf{A}_t, p_{jt}(\mathbf{A}_t, Y_t(\mathbf{A}_t))) = 0.$

The simulated changes in amounts and prices of advertising of the three merging channels from 2010 to 2013 are presented in Panel 3 of Table 10 above.³³

³³We have carefully checked that the simulated amounts of advertising are below the maximum levels imposed by the regulator.

References

- Anderson, S. P. and Coate, S. (2005). Market provision of broadcasting: A welfare analysis. The Review of Economic Studies, 72(4):947–972.
- Argentesi, E. and Filistrucchi, L. (2007). Estimating market power in a two-sided market: The case of newspapers. Journal of Applied Econometrics, 22(7):1247–1266.
- Armstrong, M. (2006). Competition in two-sided markets. The RAND Journal of Economics, 37(3):668-691.
- Ashenfelter, O. and Hosken, D. (2010). The effect of mergers on consumer prices: Evidence from five mergers on the enforcement margin. *Journal of Law and Economics*, 53(3):417 466.
- Ashenfelter, O. C., Hosken, D. S., and Weinberg, M. C. (2013). The price effects of a large merger of manufacturers: A case study of Maytag-Whirlpool. American Economic Journal: Economic Policy, 5(1):239-61.
- Baker, J. B. and Bresnahan, T. F. (1985). The gains from merger or collusion in productdifferentiated industries. *The Journal of Industrial Economics*, 33(4):427-444.
- Berndt, E. R. (1991). The Practice of Econometrics: Classic and Contemporary. Addison-Wesley Publishing Company.
- Berndt, E. R. and Wood, D. O. (1975). Technology, prices, and the derived demand for energy. The Review of Economics and Statistics, 57(3):259-68.
- Berry, S., Eizenberg, A., and Waldfogel, J. (2016). Optimal product variety in radio markets. *The RAND Journal of Economics*, 47(3):463–497.
- Berry, S. T. (1994). Estimating discrete-choice models of product differentiation. The RAND Journal of Economics, pages 242–262.
- Björnerstedt, J. and Verboven, F. (2016). Does merger simulation work? Evidence from the Swedish analgesics market. American Economic Journal: Applied Economics, 8(3):125-64.
- Borenstein, S. (1990). Airline mergers, airport dominance, and market power. American Economic Review, 80(2):400-404.
- Chen, Y. and Gayle, P. G. (2019). Mergers and product quality: Evidence from the airline industry. International Journal of Industrial Organization, 62:96 - 135.
- Christensen, L. R., Jorgenson, D. W., and Lau, L. J. (1973). Transcendental logarithmic production frontiers. *The Review of Economics and Statistics*, 55(1):28-45.
- Cournot, A. (1838). Recherches sur les principes mathématiques de la théorie de la richesse. Hachette, Paris.
- Crawford, G., Smith, J., Sturgeon, P., and Deer, L. (2017). The (inverse) demand for advertising in the UK: Should there be more advertising on television? Working paper, University of Warwick.
- Cunningham, B. M. and Alexander, P. J. (2004). A theory of broadcast media concentration and commercial advertising. *Journal of Public Economic Theory*, 6(4):557–575.

- Economides, N. and Salop, S. C. (1992). Competition and integration among complements, and network market structure. *Journal of Industrial Economics*, 40(1):105–23.
- Fan, Y. (2013). Ownership consolidation and product characteristics: A study of the US daily newspaper market. The American Economic Review, 103(5):1598-1628.
- Focarelli, D. and Panetta, F. (2003). Are mergers beneficial to consumers? Evidence from the market for bank deposits. *American Economic Review*, 93(4):1152–1172.
- Hastings, J. and Gilbert, R. (2005). Market power, vertical integration and the wholesale price of gasoline^{*}. Journal of Industrial Economics, 53(4):469-492.
- Hastings, J. S. (2004). Vertical relationships and competition in retail gasoline markets: Empirical evidence from contract changes in southern California. American Economic Review, 94(1):317– 328.
- Hausman, J., Leonard, G., and Zona, J. D. (1994). Competitive analysis with differentiated products. Annales d'Economie et de Statistique, (34):159–180.
- Hosken, D., Silvia, L., and Taylor, C. (2011). Does concentration matter? Measurement of petroleum merger price effects. *The American Economic Review*, 101(3):45–50.
- Hurwicz, L. and Uzawa, H. (1971). On the integrability of demand functions. In Chipman, J. et al., editors, *Preferences, utility and demand*. Harcourt, Brace, Jovanovich, New York.
- Ivaldi, M. and Muller-Vibes, C. (2018). The differentiated effect of advertising on readership: Evidence from a two-sided market approach. *Marketing Letters*, 29(3):363–376.
- Jeziorski, P. (2014). Effects of mergers in two-sided markets: The US radio industry. American Economic Journal: Microeconomics, 6(4):35-73.
- Kaiser, U. and Wright, J. (2006). Price structure in two-sided markets: Evidence from the magazine industry. *International Journal of Industrial Organization*, 24(1):1–28.
- Kim, E. H. and Singal, V. (1993). Mergers and market power: Evidence from the airline industry. American Economic Review, 83(3):549-69.
- McFadden, D. (1978). Modelling the choice of residential location. Institute of Transportation Studies, University of California.
- Nevo, A. (2000). Mergers with differentiated products: The case of the ready-to-eat cereal industry. The RAND Journal of Economics, 31(3):395-421.
- Nilssen, T. and Sørgard, L. (2000). TV advertising, programming investments, and product-market oligopoly. *Papers 6/2000, Norwegian School of Economics and Business Administration*.
- Rochet, J.-C. and Tirole, J. (2003). Platform competition in two-sided markets. Journal of the European Economic Association, 1(4):990–1029.
- Rysman, M. (2004). Competition between networks: A study of the market for yellow pages. *The Review of Economic Studies*, 71(2):483–512.
- Small, K. and Rosen, H. (1981). Applied welfare economics with discrete choice models. *Econo-metrica*, 49(1):105–30.

- Sweeting, A. (2010). The effects of mergers on product positioning: Evidence from the music radio industry. The RAND Journal of Economics, 41(2):372–397.
- Verboven, F. (1996). International price discrimination in the European car market. The RAND Journal of Economics, 27(2):240–268.
- Werden, G. J. and Froeb, L. M. (1994). The effects of mergers in differentiated products industries: Logit demand and merger policy. *Journal of Law, Economics, Organization*, 10(2):407-426.
- Wilbur, K. C. (2008). A two-sided, empirical model of television advertising and viewing markets. Marketing Science, 27(3):356–378.
- Wilbur, K. C., Goeree, M. S., and Geert, R. (2009). Effects of advertising and product placement on television audiences. *Working paper ISSN 1424-0459*.
- Williams, H. C. (1977). On the formation of travel demand models and economic evaluation measures of user benefit. *Environment and planning* A, 9(3):285-344.
- Zhang, J. (2019). Regulating advertising quantity: Is it efficient? NET Institute Working Paper No. 16-06.